# Optimization for Buffer and Splitter Insertion in AQFP Circuits with Local and Group Movement 

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## Outline

> AQFP Circuit
> Problem Formulation
> Optimization Methods
> Overall Flow
> Experimental Results
> Conclusion

## AQFP Circuit

> Adiabatic quantum-flux parametron (AQFP) is a superconducting technology with extremely low power consumption compared to traditional CMOS technology
> Special constraints

1) Fanout branching: each logic gate and buffer can only drive one output, and each splitter can drive multiple outputs no more than the given splitting capacity $s p$
2) Path balancing: for each node, its input values must be released by nodes at its previous level

## > Assumptions

1) Primary inputs (PIs) are aligned at the same level
2) Primary outputs (POs) are aligned at the same level
3) PIs should satisfy the fanout branching constraint

## AQFP Circuit

> Example (a netlist we want to convert to an legal AQFP circuit)


## AQFP Circuit

$>$ Example (solving fanout branching constraint, assume $s p=2$ )


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$>$ Example (solving fanout branching constraint, assume $s p=2$ )


## AQFP Circuit

$>$ Example (PI alignment and PO alignment)


## AQFP Circuit

$>$ Example (solving path balancing constraint)


## Problem Formulation

$>$ Input

1) A netlist $N$
2) Splitting capacity $s p$
$>$ Output

- An AQFP circuit $C$ which exhibits the same functionality as $N$ and satisfies all the constraints and assumptions
$>$ Target
- Minimize the cost (number of inserted buffers and splitters) of the output circuit


## Optimization Methods

> Backward Movement Optimization

- Backward Group Movement
- Input Modifying Backward Movement
> Forward Movement Optimization
- Forward Group Movement
- Buffer Integrating Forward Movement
> Level Perturbation
- Flexibility-driven Branching Tree
- Forced Movement
- Fanout-pair Level Adjustment


## Backward Group Movement

$>$ A group is a set of gate(s) and splitter(s) which form a connected subgraph in an AQFP circuit
the set of the red nodes is a group


## Backward Group Movement

> In backward movement optimization, we want to move logic gates backward for reducing the number of buffers


## Backward Group Movement

$>$ However, the movement of a gate $g$ may be blocked by other splitters, gates or previously created groups

- Cluster $g$ and "the gates, the splitters, and the groups blocking $g$ 's movement" into a new group, and perform group movement
- Only the movement which do not increase the number of buffers will be accepted
- The method for deciding the order of the movements of gates is detailed in the paper


## Backward Group Movement

$>$ If we first try to move $g_{1}$ backward


## Backward Group Movement

$>$ Try to move the group $\left\{g_{1}, S\right\}$ backward, but the result will NOT be accepted


## Backward Group Movement

$>$ Suppose we try to move $g_{2}$ backward next, with the previously created group retained in the circuit


## Backward Group Movement

$>$ Try to move the group $\left\{g_{1}, g_{2}, S\right\}$ backward, and the result will be accepted


## Optimization Methods

> Backward Movement Optimization

- Backward group movement
- Input modifying backward movement
> Forward Movement Optimization
- Forward group movement
- Buffer integrating forward movement
> Level Perturbation
- Flexibility-driven branching tree
- Forced movement
- Fanout-pair level adjustment


## Input Modifying Backward Movement

> Modify the input edge(s) of a gate so we can move it backward easier


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## Forward Group Movement

> Use similar rules in "backward group movement" to construct groups and move them forward

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## Buffer Integrating Forward Movement

> Move groups without splitters forward, and try to integrate buffers into less splitters if possible


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## Flexibility-driven Branching Tree

$>$ A branching tree of a gate or PI $g$ is a set of nodes containing

1) $g$
2) the gates and POs that $g$ passes its output signal to
3) the buffers and splitters between (1) and (2)
> Minimum branching tree

- Advantage: requires the least number of buffers and splitters
- Disadvantage: the movement flexibility of gates is lower


## Flexibility-driven Branching Tree

$>$ The minimum branching tree of $i_{1}$

- The movement of $\mathrm{g}_{4}$ is blocked by a splitter



## Flexibility-driven Branching Tree

> Flexibility-driven branching tree

- Advantage: the movement flexibility of gates is higher
- Disadvantage: use as many buffers as possible (higher cost)


## Flexibility-driven Branching Tree

$>$ The flexibility-driven branching tree of $i_{1}$

- The movement of $g_{4}$ is NOT blocked by any gate or splitter



## Optimization Methods

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## Forced Movement

$>$ Force a gate to be moved backward one level, and resolve the created violations


## Forced Movement

$>$ Force a gate to be moved backward one level, and resolve the created violations


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## Fanout-pair Level Adjustment

> For gates $s$ and $l$ in the same branching tree (assume $s$ is at a smaller level than that of $l$ ), move $s$ forward one level and move $l$ backward one level, then resolve

the movement of $\mathrm{g}_{2}$ is NOT blocked beffarradidgurtronent


## Experimental Results

$>$ Compare to state-of-the-art methods

- A Global Optimization Algorithm for Buffer and Splitter Insertion in Adiabatic Quantum-Flux-Parametron Circuits [3]

1) Use integer linear programming-based method to decide logic gates levels
2) Use dynamic programming-based method to insert buffers and splitters

- Depth-Optimal Buffer and Splitter Insertion and Optimization in AQFP Circuits [2]

1) Obtained depth-optimal circuits
2) Use retiming-based method to move gates and splitters for cost reduction

## Experimental Results

## > Optimal solution

| Benchmark | Original Circuit |  |  | Opt from [1] |  | [3] |  | [2] |  |  | Our method |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Gates | $\max \|\mathrm{LO}\|$ | D | \#B/S | D' | \#B/S | D' | \#B/S | D' | Time(s) | \#B/S | D' | Time(s) |
| adder1 | 7 | 2 | 4 | 16* | 8 | - | - | 16* | 8 | <0.01 | 16* | 8 | <0.01 |
| adder8 | 77 | 3 | 17 | 371* | 33 | - | - | 371* | 33 | <0.01 | 371* | 33 | $<0.01$ |
| counter16 | 29 | 4 | 9 | 65* | 17 | 66 | 17 | 65* | 17 | <0.01 | 65* | 17 | <0.01 |
| counter32 | 82 | 4 | 13 | 154* | 23 | 156 | 23 | 154* | 23 | <0.01 | 154* | 23 | $<0.01$ |
| counter64 | 195 | 4 | 17 | 347* | 30 | 351 | 30 | 347* | 30 | <0.01 | 347* | 30 | $<0.01$ |
| counter128 | 428 | 4 | 22 | 747* | 38 | 755 | 38 | 747* | 38 | 0.01 | 747* | 38 | 0.01 |
| sorter32 | 480 | 2 | 15 | 480* | 30 | - | - | 480* | 30 | <0.01 | 480* | 30 | <0.01 |
| sorter48 | 880 | 3 | 20 | 880* | 35 | - | - | 880* | 35 | 0.01 | 880* | 35 | 0.01 |
| mult8 | 439 | 9 | 35 | - | - | 1681 | 70 | 1709 | 70 | 0.05 | 1680 | 70 | 0.04 |
| c17 | 6 | 2 | 3 | 12* | 5 | - | - | 12* | 5 | <0.01 | 12* | 5 | <0.01 |
| c432 | 121 | 10 | 26 | - | - | 829 | 37 | 839 | 37 | 0.01 | 829 | 37 | <0.01 |
| c499 | 387 | 8 | 18 | - | - | 1173 | 29 | 1173 | 29 | 0.03 | 1177 | 29 | 0.01 |
| c880 | 306 | 9 | 27 | - | - | 1536 | 40 | 1511 | 40 | 0.07 | 1517 | 40 | 0.03 |
| c1355 | 389 | 9 | 18 | - | - | 1186 | 29 | 1184 | 29 | 0.03 | 1182 | 29 | 0.02 |
| c1908 | 289 | 14 | 21 | - | - | 1253 | 34 | 1236 | 34 | 0.04 | 1236 | 34 | 0.01 |
| c2670 | 368 | 32 | 21 | - | - | 1869 | 28 | 1940 | 28 | 0.07 | 1914 | 28 | 0.03 |
| c3540 | 794 | 38 | 32 | - | - | 1963 | 52 | 1966 | 52 | 0.11 | 1993 | 52 | 0.11 |
| c5315 | 1302 | 41 | 26 | - | - | 5505 | 40 | 5635 | 40 | 0.32 | 5584 | 40 | 0.16 |
| c6288 | 1870 | 17 | 89 | - | - | 8832 | 179 | 9009 | 179 | 0.2 | 8632 | 179 | 0.18 |
| c7552 | 1394 | 170 | 33 | - | - | 6768 | 58 | 7832 | 56 | 0.66 | 6614 | 56 | 0.42 |
| alu32 | 1513 | 128 | 100 | - | - | 13976 | 169 | 13842 | 169 | 0.59 | 13804 | 169 | 0.65 |

## Experimental Results

## > Compare to [3] (11 better, 4 worse)

| Benchmark | Original Circuit |  |  | Opt from [1] |  | [3] |  | [2] |  |  | Our method |  |  |
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| c5315 | 1302 | 41 | 26 | - | - | 5505 | 40 | 5635 | 40 | 0.32 | 5584 | 40 | 0.16 |
| c6288 | 1870 | 17 | 89 | - | - | 8832 | 179 | 9009 | 179 | 0.2 | 8632 | 179 | 0.18 |
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## Experimental Results

## > Compare to [2] (8 better, 3 worse)

| Benchmark | Original Circuit |  |  | Opt from [1] |  | [3] |  | [2] |  |  | Our method |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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## Conclusion

$>$ For optimizing the buffer and splitter insertion problem in AQFP circuits, we proposed

1) Movement methods
2) Level perturbation methods
$>$ Compared to state of the art [2] and [3], our method obtained better results with less runtime in most of the benchmarks

## Experimental Results in Large Benchmarks

> Benchmarks with number of logic gates range from $4000 \sim 130000$

|  | Initial |  | [2] |  |  |  | Our Method |  |  | Improvement |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Benchmark | \#gates | depth |  | \#B/S | depth | time (s) | \#B/S | depth | time (s) | \#B/S | time |
| sin | 4303 | 110 |  | 14783 | 188 | 2.43 | 14685 | 188 | 1.02 | $0.66 \%$ | $58.02 \%$ |
| arbiter | 7000 | 59 |  | 25725 | 63 | 0.75 | 25731 | 63 | 2 | $-0.02 \%$ | $-166.67 \%$ |
| voter | 7860 | 47 |  | 15736 | 86 | 0.5 | 15810 | 86 | 0.67 | $-0.47 \%$ | $-34.00 \%$ |
| square | 12180 | 126 |  | 63087 | 251 | 10.6 | 65602 | 251 | 6.8 | $-3.99 \%$ | $35.85 \%$ |
| multiplier | 19710 | 133 |  | 61714 | 264 | 43.76 | 65420 | 264 | 10.99 | $-6.01 \%$ | $74.89 \%$ |
| log2 | 24456 | 200 |  | 84440 | 379 | 48.76 | 84215 | 379 | 32.83 | $0.27 \%$ | $32.67 \%$ |
| mem_ctrl | 42758 | 73 |  | 213463 | 114 | 95.78 | 185443 | 114 | 38.68 | $13.13 \%$ | $59.62 \%$ |
| sqrt | 23238 | 3366 |  | 1323854 | 6628 | 890.73 | 1317608 | 6628 | 34.03 | $0.47 \%$ | $96.18 \%$ |
| div | 57300 | 2217 |  | 1617032 | 4371 | 2190.5 | 1373661 | 4371 | 102.68 | $15.05 \%$ | $95.31 \%$ |
| hyp | 136109 | 8762 |  | 5596808 | 17246 | 2610 | 5479479 | 17246 | 402.91 | $2.10 \%$ | $84.56 \%$ |

## Different Minimum Branching Trees

$>$ Hard to predict which one is more helpful for movements

minimum branching tree A

minimum branching tree B

## Buffer Integration in Backward Movement

> Using more splitters would decrease the movability of gates


