



Computing Architecture for Large Language Models (LLMs) and Large Multimodal Models (LMMs)

Bor-Sung Liang

MediaTek

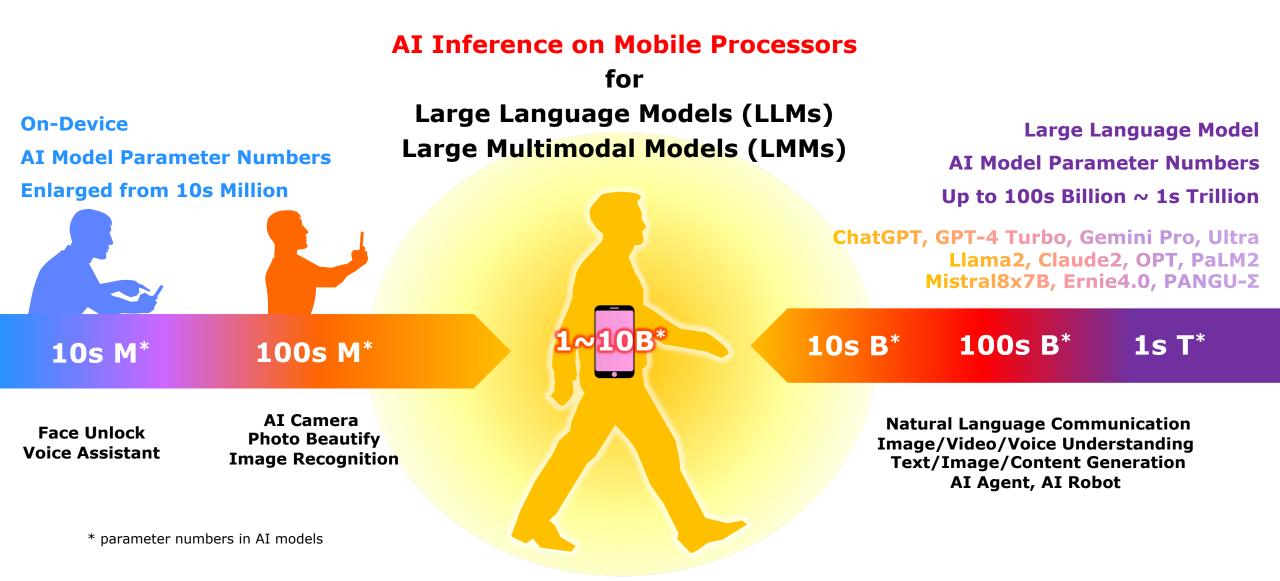
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Motivation

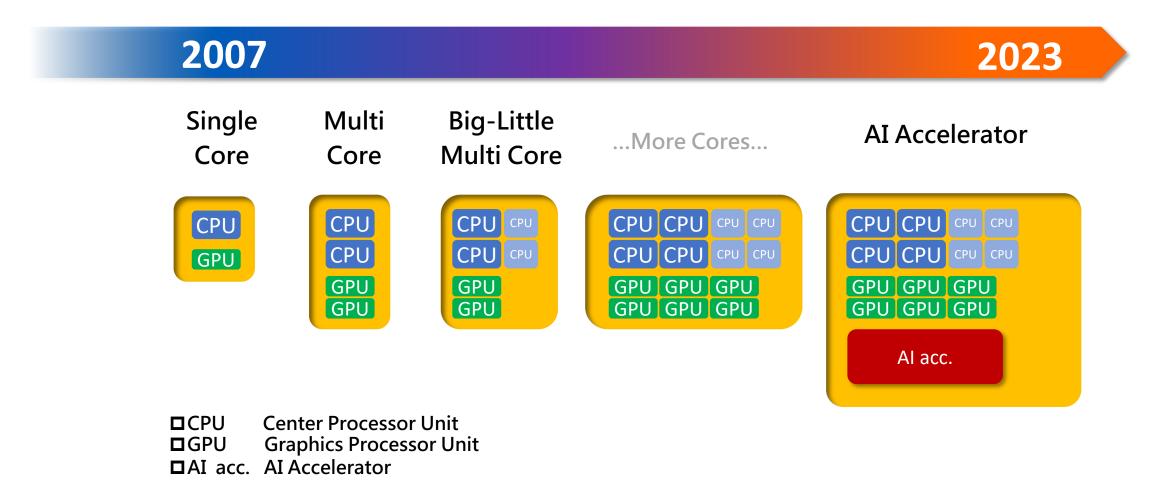


Trends of Mobile Processors and Al Models

Trends of Mobile Processor in a Decade

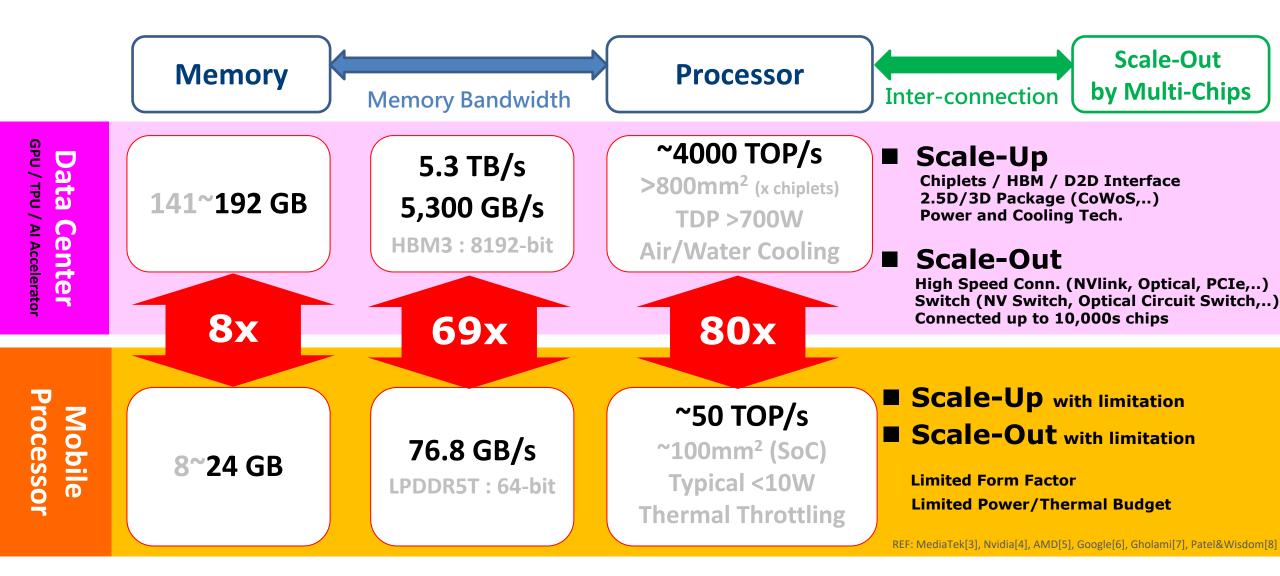


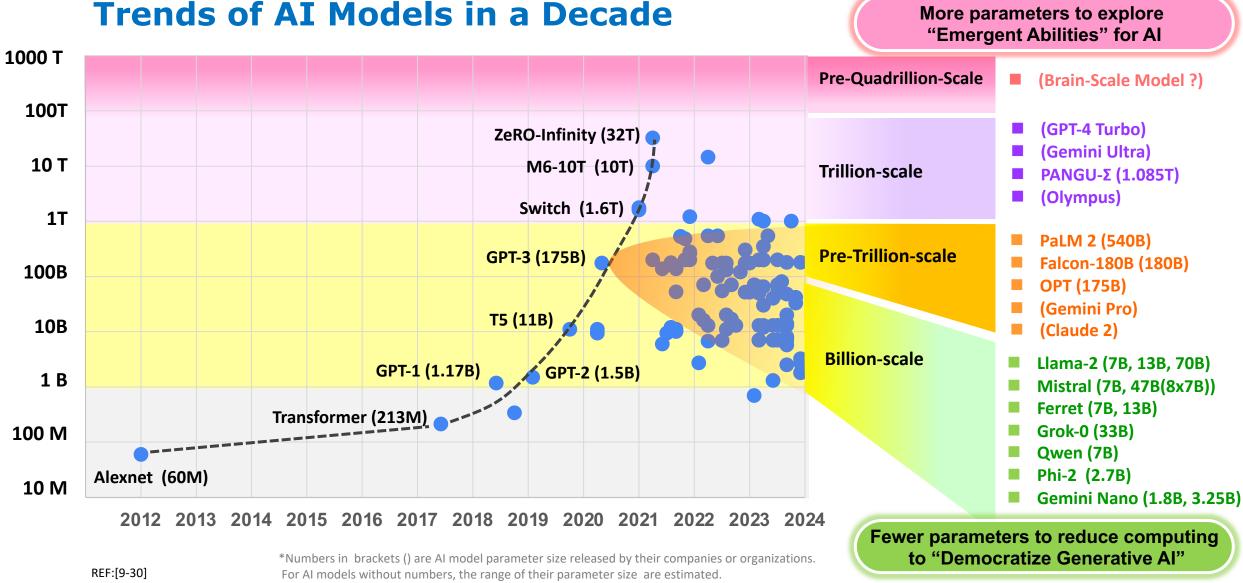
Trends of Computing Architecture in Mobile Processor



*The number of CPU, GPU, and AI accelerator cores is for reference. Each application processor will have different architecture and number depending on the actual situation.

More Limitations on Mobile Processor for AI Computing

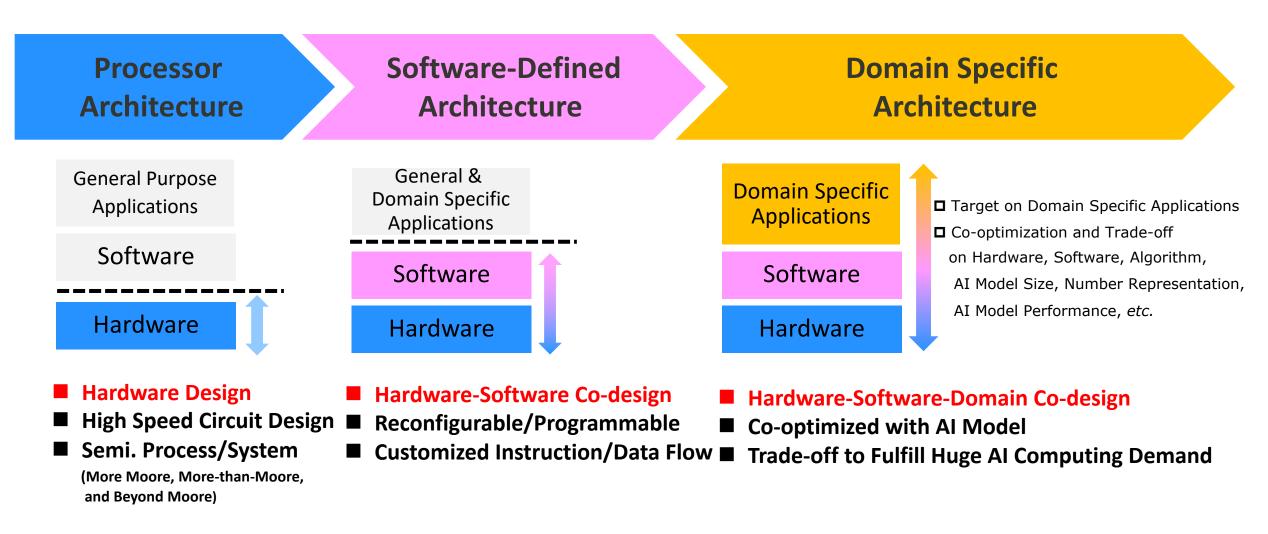




More parameters to explore

Domain Specific Architecture Design for Al Inference

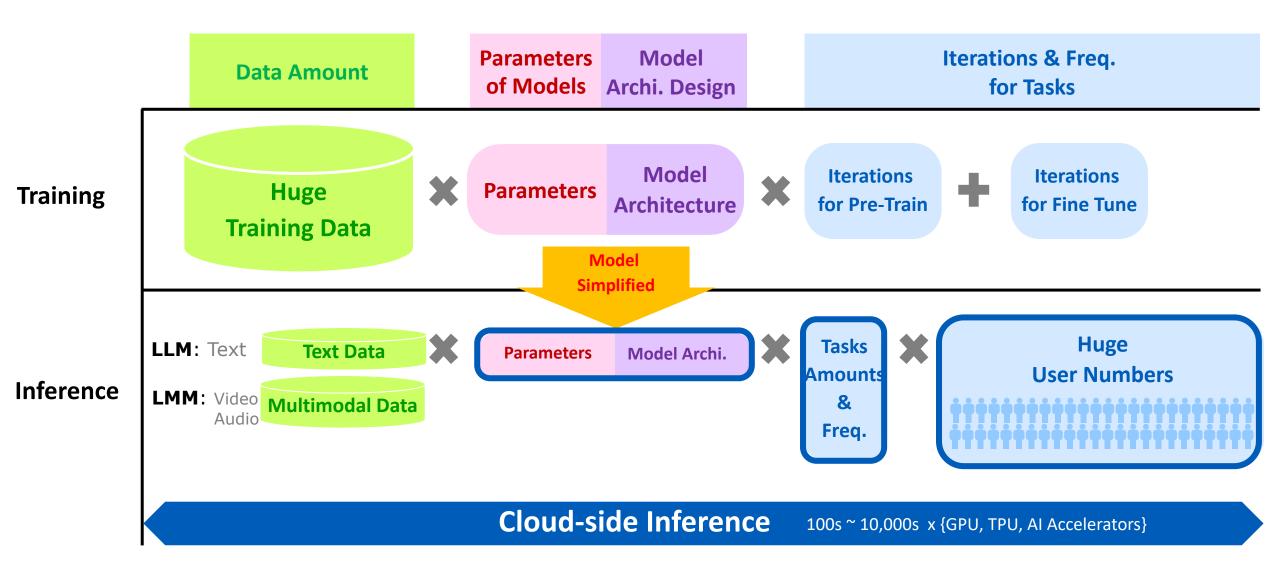
Trends for Architecture Design : Domain Specific Architecture



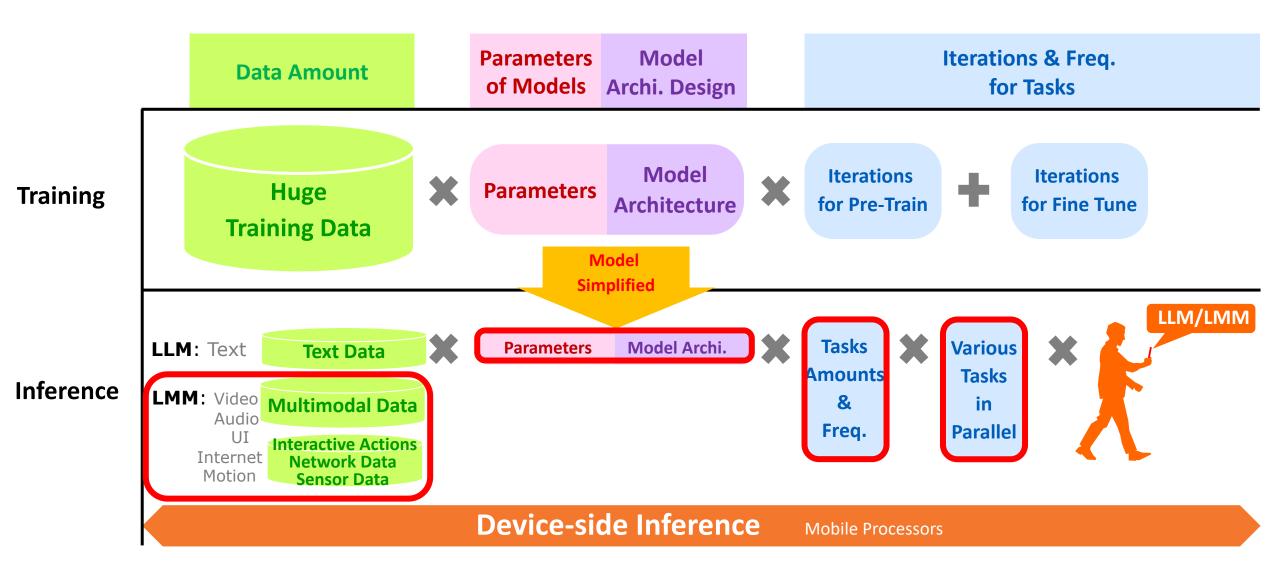
REF: Hennessy & Patterson [1], IRDS [2]

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AI Computing for Cloud-side Inference



AI Computing for Device-side Inference



Techniques to Reduce AI Model Size

To Reduce Memory Footprint in Storage and Computing Cost

Number Representation

- Quantization / Reducing the precision
- □ 32-bit (FP32) \rightarrow 16-bit (FP16, BF16) \rightarrow 8-bit (INT8, FP8) \rightarrow 4-bit (INT4) ...

Use Smaller LLM/LMM by Knowledge Distillation (KD)

□ Utilize a full-size model (teacher) to train a smaller model (student)

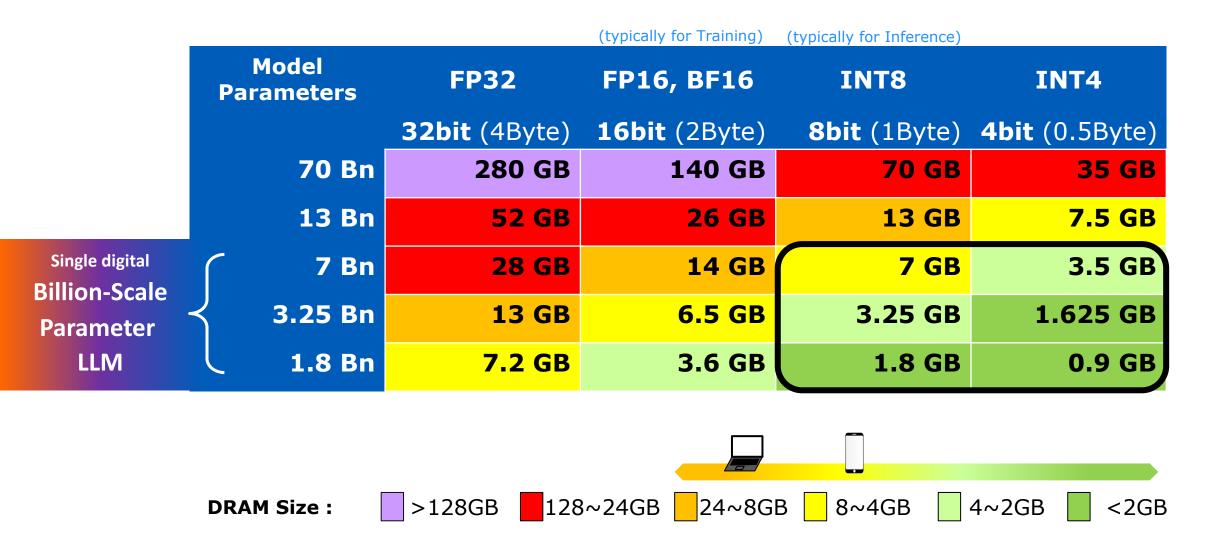
Sparsity / Pruning

□ Increase zero weights in model parameters

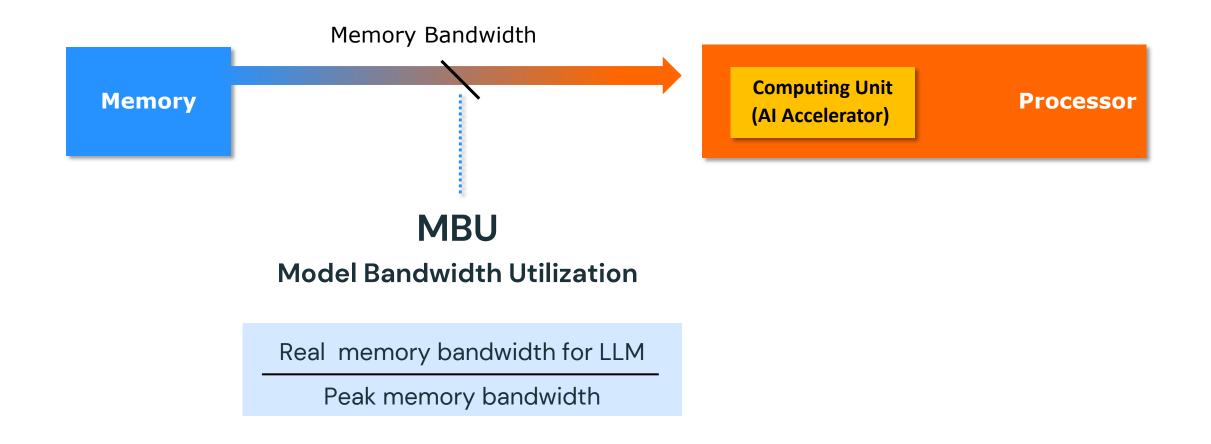
REF: Dally[31], Dean&Vahdat[32], Hinton et al [33], Naffziger[34]

* not an exhaustive list

Model Size for different Parameter and Number Representation

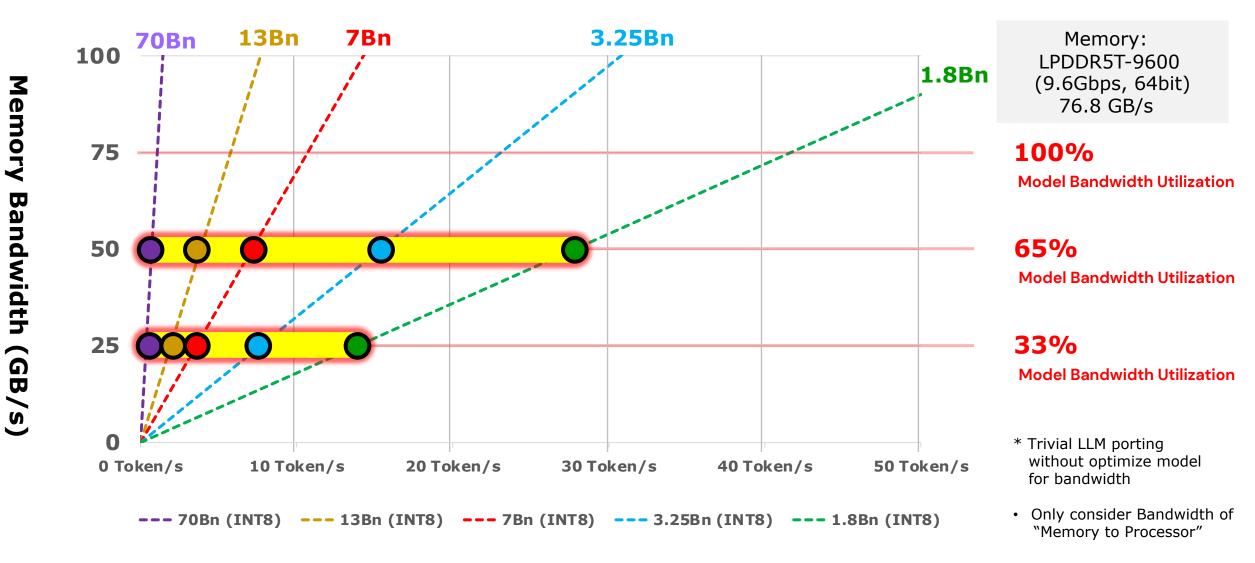


Bandwidth Utilization Ratio

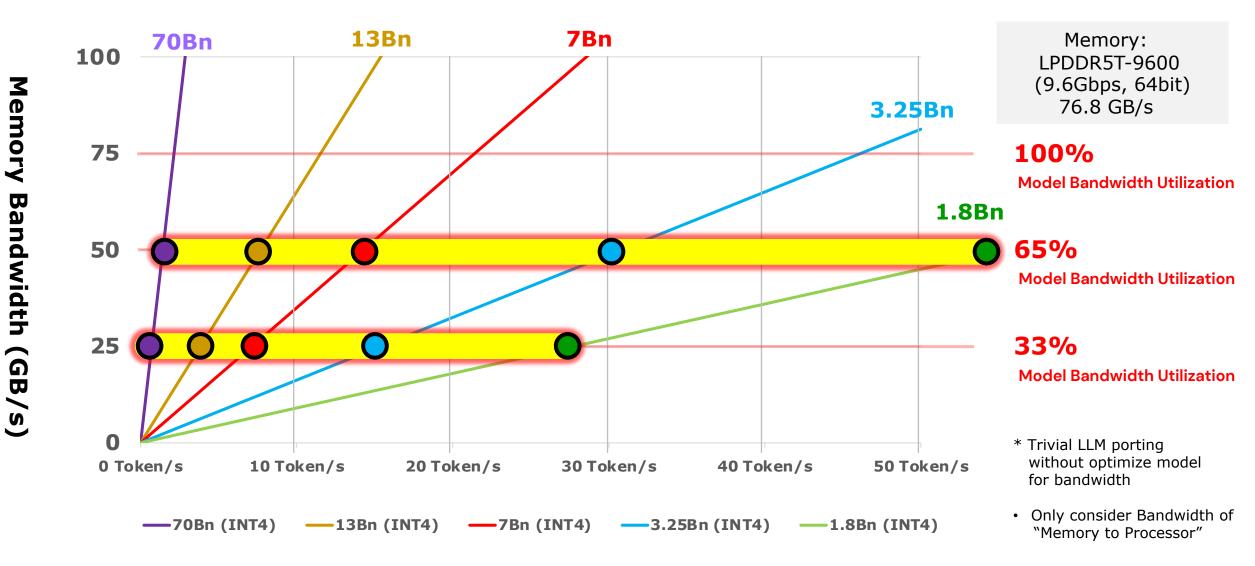


REF: Agarwal, et al [35]

Token Speed under Memory Bandwidth Limit (LLM @ INT8)



Token Speed under Memory Bandwidth Limit (LLM @ INT4)



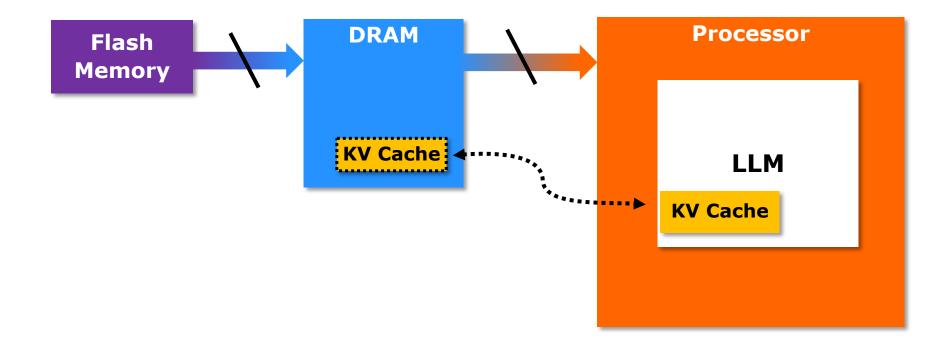
Techniques to Improve LLM/LMM Performance

- KV Cache (Key/Value cache)
- Retrieval Augmented Generation (RAG)
- Sparsity Mixture of Experts (SMoE)
- Speculative Execution
- Speculative Execution with Cloud-Device Collaboration

* not an exhaustive list

KV Cache (Key/Value Cache)

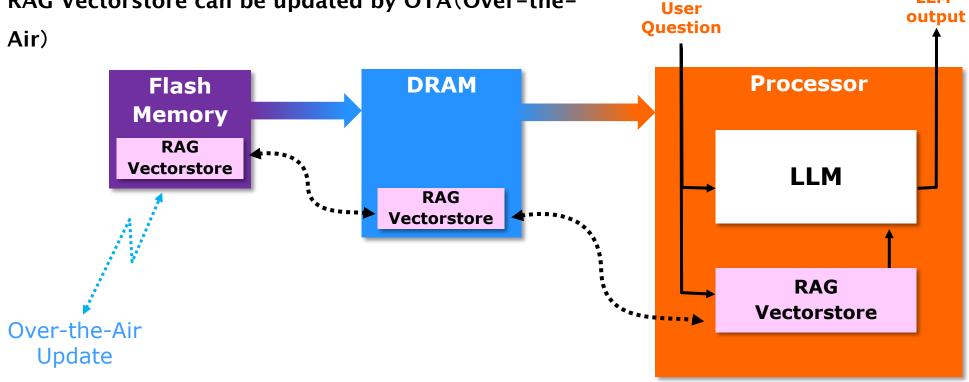
Catch previous Keys and Values to save recalculation



REF: Agarwal, et al [35], Chen [36]

Retrieval Augmented Generation (RAG)

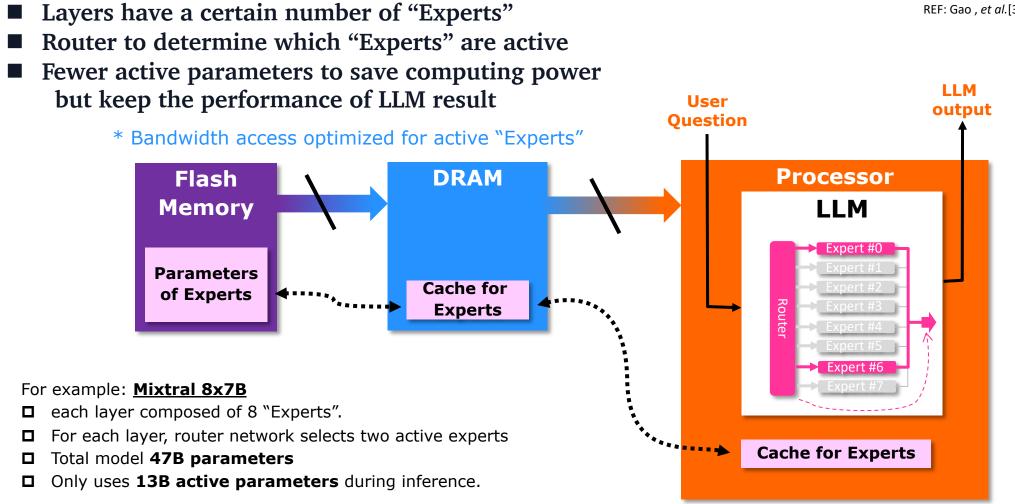
- Incorporating knowledge from external databases
- Enhances the accuracy and credibility of the models
- RAG Vectorstore can be updated by OTA(Over-the-



REF: Lewis, et al.[37]

LLM

Sparse Mixture of Experts (SMoE)

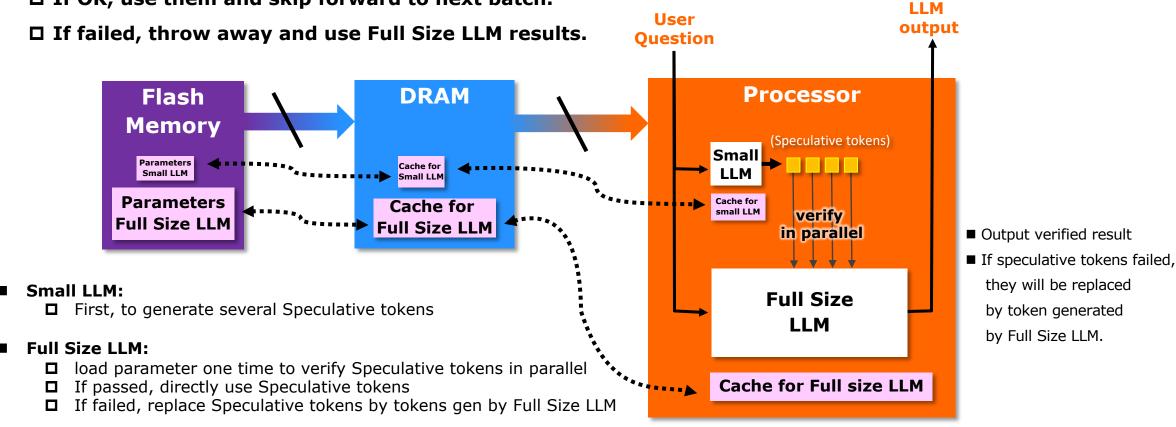


REF: Gao, et al.[31]

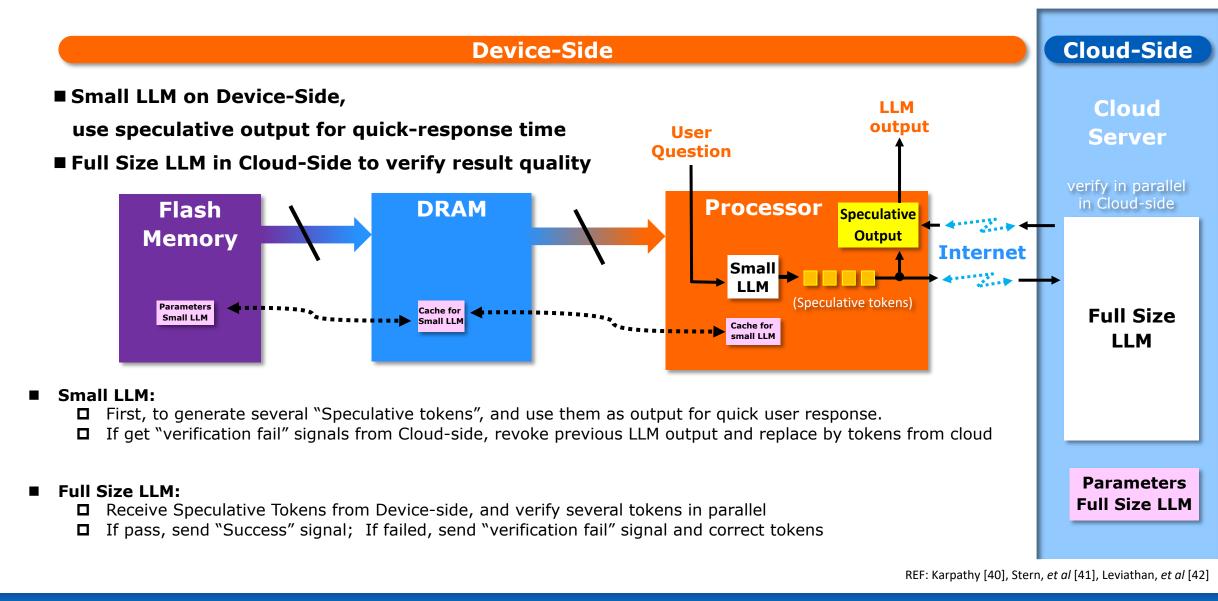
REF: Eliseev&Mazur[38], Mistral.AI [39]

Speculative Execution

- Small LLM to generate Speculative tokens
- Feed all Speculative tokens to Full Size LLM in a batch to verify
 - □ If OK, use them and skip forward to next batch.



Speculative Execution (Cloud-Device Collaboration)



Token Speed for LLM & LMM

How Fast We Read

Read word-by-word

Read Normally 250 words/min

(Adults Silent-reading Speed 238 words/min)

The International Solid-State Circuits Conference (ISSCC) is an esteemed annual gathering that serves as a global platform for the presentation of cutting-edge advancements in solid-state circuits and systems-on-a-chip. It is renowned for showcasing the latest research and breakthroughs in integrated circuits, drawing engineers, researchers, and industry professionals from across the globe.

At ISSCC, the technology sessions cover a wide range of topics, including:

- Advanced semiconductor technologies
- Innovative circuit designs and architectures
- Trends in system-on-chip (SoC) integration
- High-speed communication and data processing
- Low-power and energy-efficient circuitry
- Silicon photonics and optoelectronic devices
- Novel sensor technologies
- Emerging memory technologies

Read Skimminglooking only for the general or main ideasRead Scanninglook only for a specific information

Read Proficiently 1000 words/min

(Skimming speeds of 1000+ words/min)

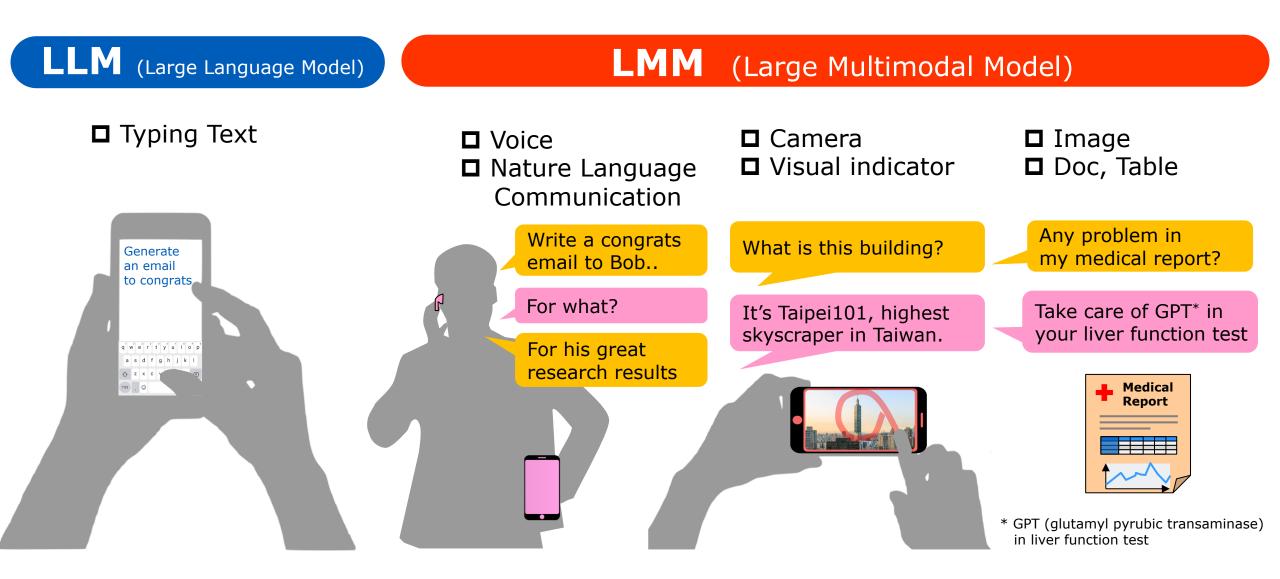
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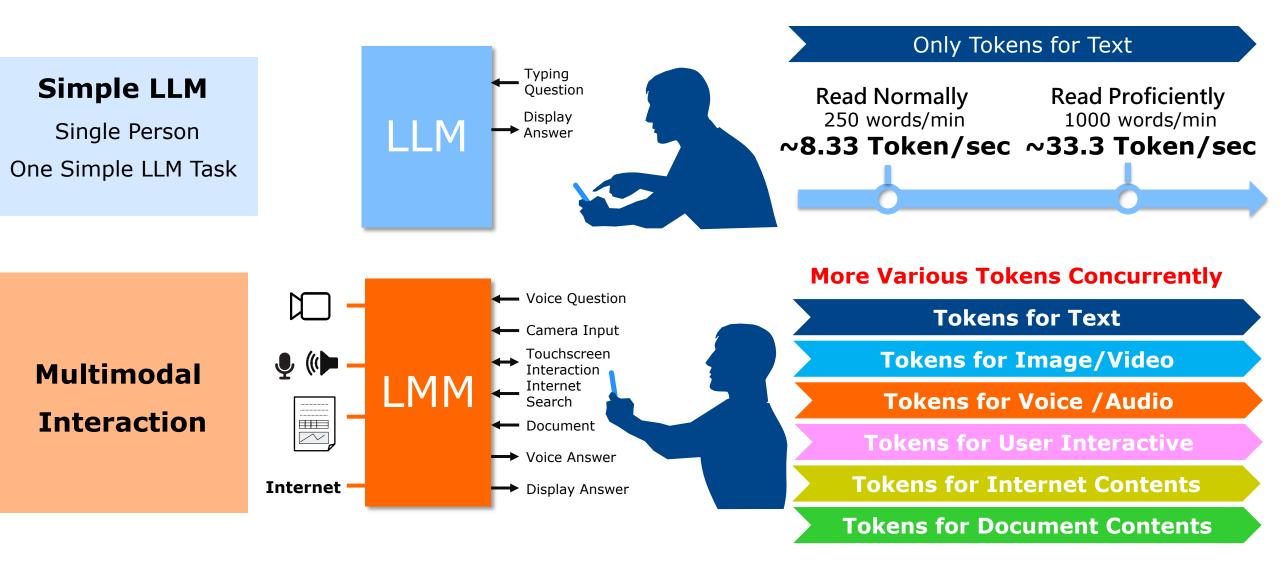
- Advanced semiconductor technologies
- Innovative circuit designs and architectures
- Trends in system-on-chip (SoC) integration
- High-speed communication and data processing
- Low-power and energy-efficient circuitry
- Silicon photonics and optoelectronic devices
- Novel sensor technologies
- Emerging memory technologies

REF: Brysbaert [43]

LLM and LMM in Mobile Devices

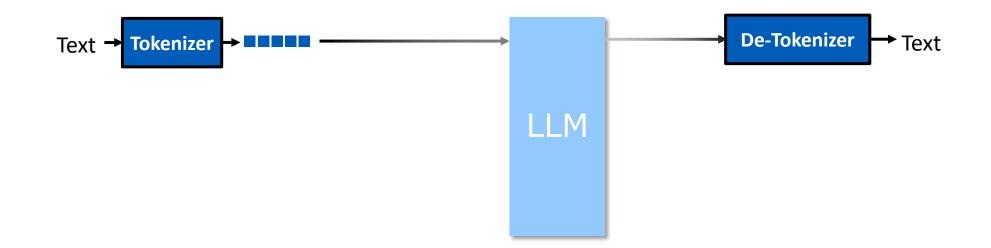


Types of Tokens in LLM & LMM



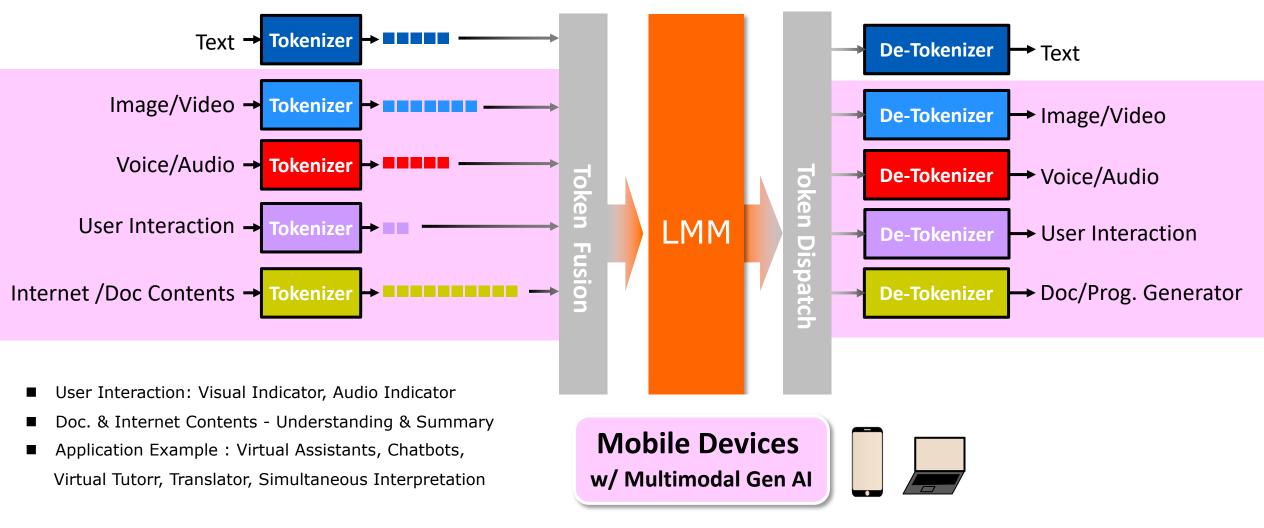
REF: [44-47]

Token Process of LLM



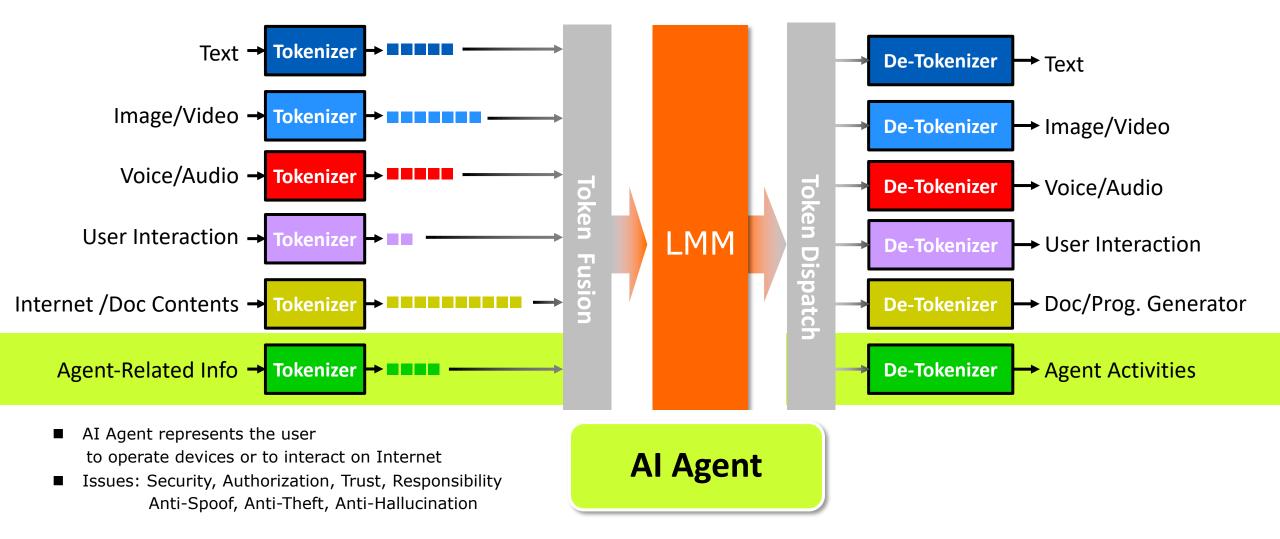


Token Process of LMM for Multimodal Generative AI



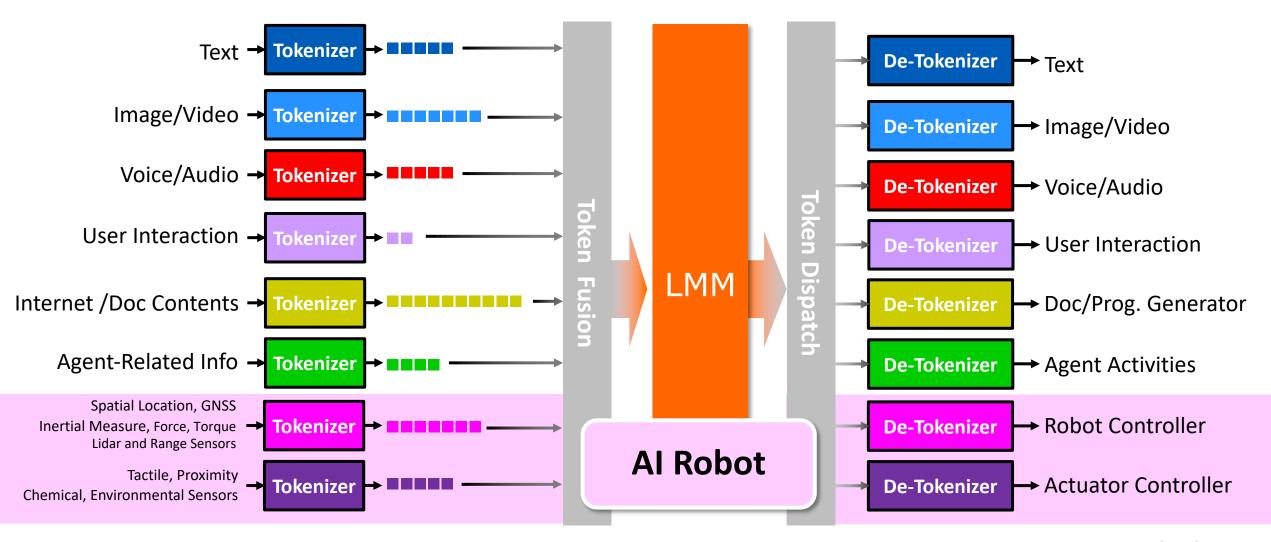
REF: [44-47]

Token Process of LMM for AI Agent



REF: Yan, et al [48], Durante, et al [49]

Token Process of LMM for AI Robotics

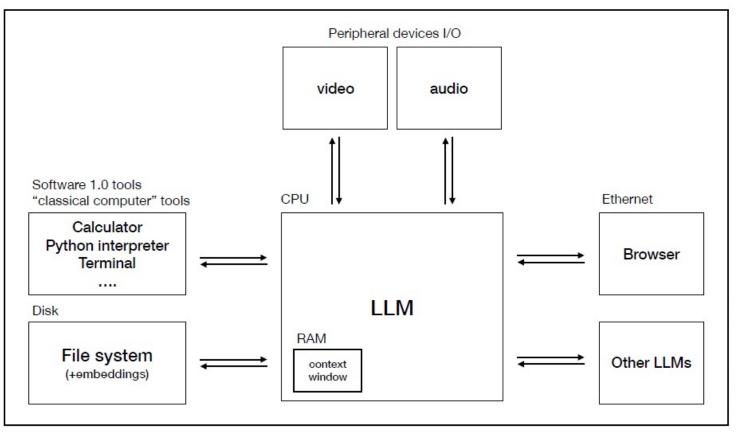


REF: [50-52]

LLM / LMM Collaboration with Mobile OS and Cloud

Concept of LLM OS

LLM OS



Courtesy : Andrej Karpathy

REF: Karpathy [53]

Issues for LLM OS

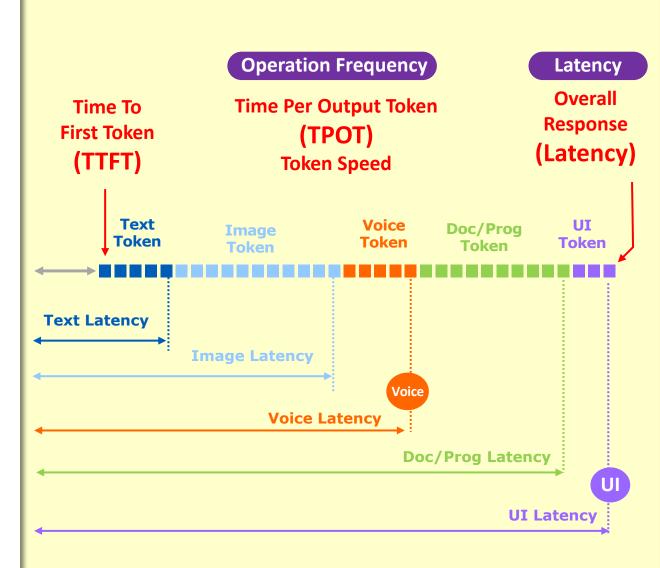
Operation Speed

- LLM :~10s token/sec
- Mobile OS : time measured in ms
 ~1000 Ticks /sec
 (if time interrupt for every 1 ms)

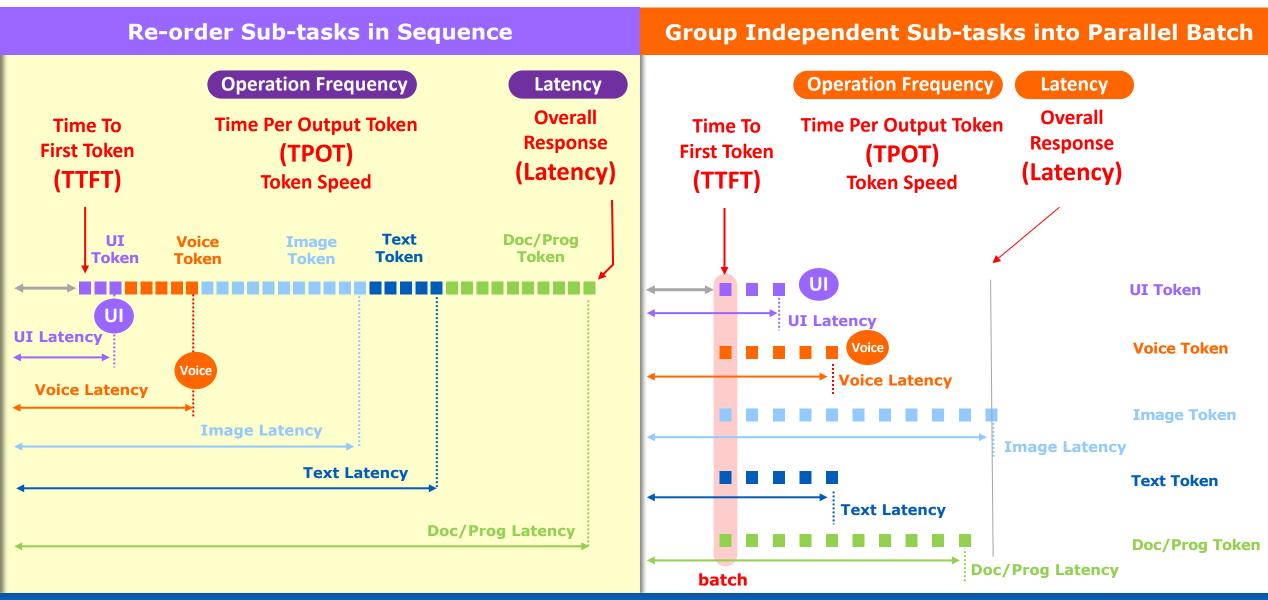
Realtime

- Overall time to finish a Task
- Time to finish Sub-tasks
- Interrupt
- Multi-thread / Task Switch

Priority

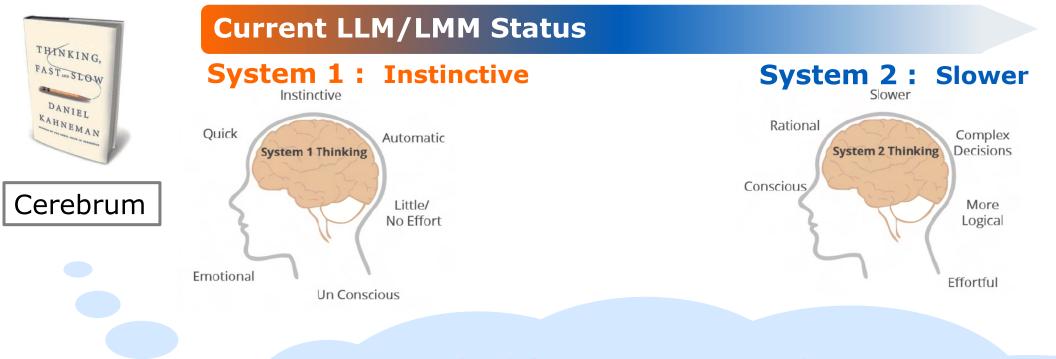


LLM OS: Re-ordering and Parallel Batch



ISPD 2024 Computing Architecture for Large-Language Models (LLMs) and Large Multimodal Models (LMMs)

Current LLM/LMM : from "System 1" to "System 2"

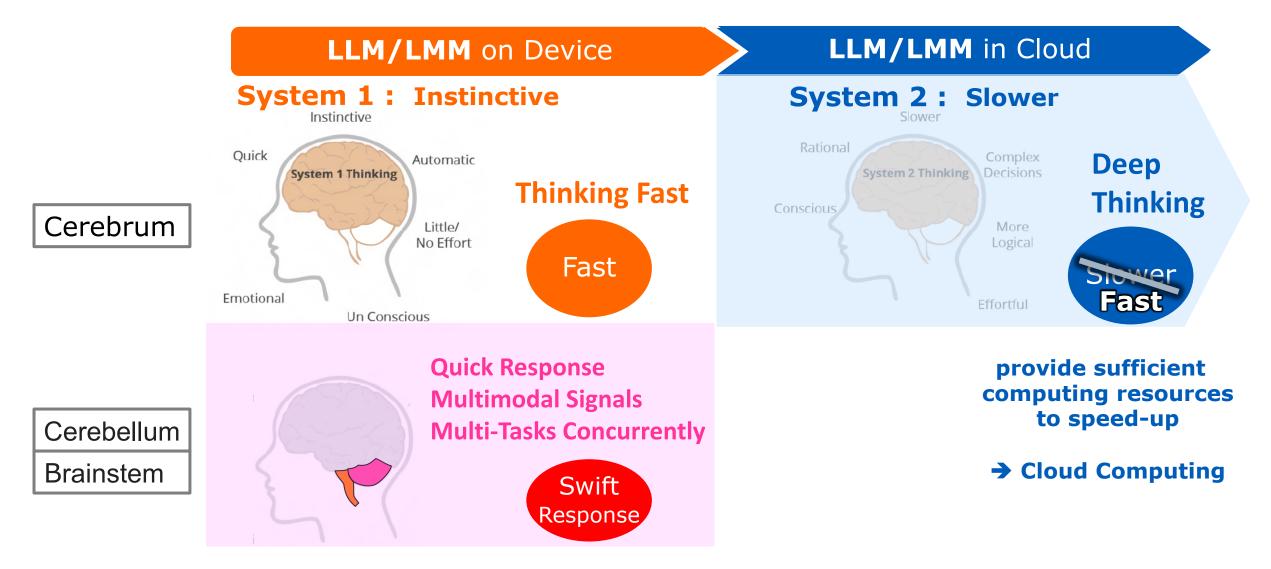


Inspired from System 1 and 2 :

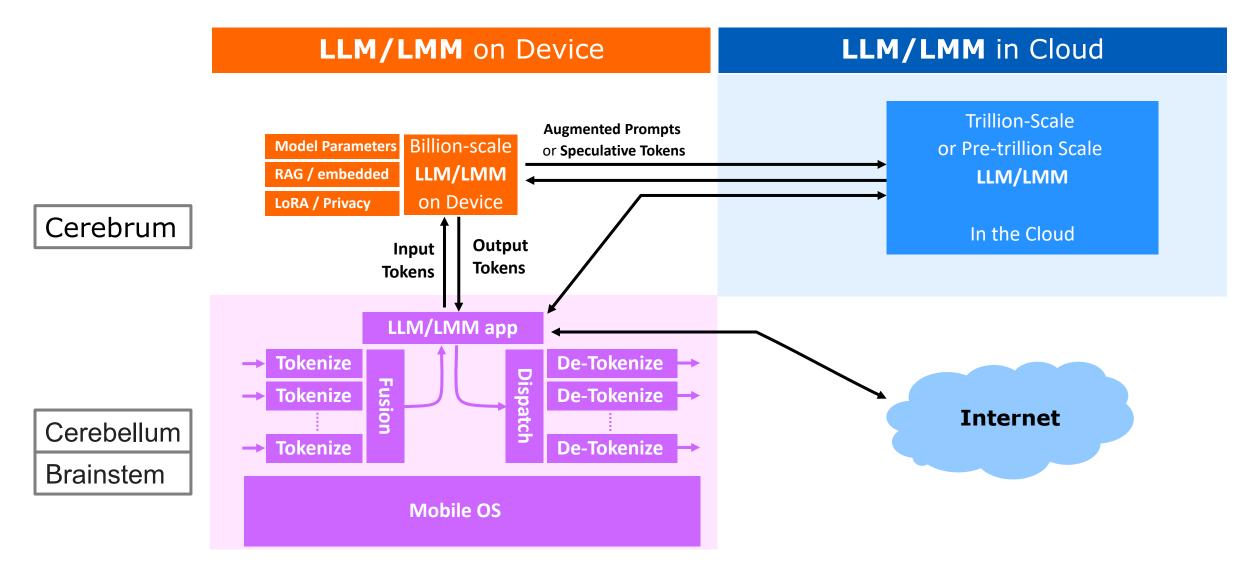
Can we collaborate both Device-side and Cloud-side for System 1 and 2?

REF: Karpathy [53], Kahneman [54]

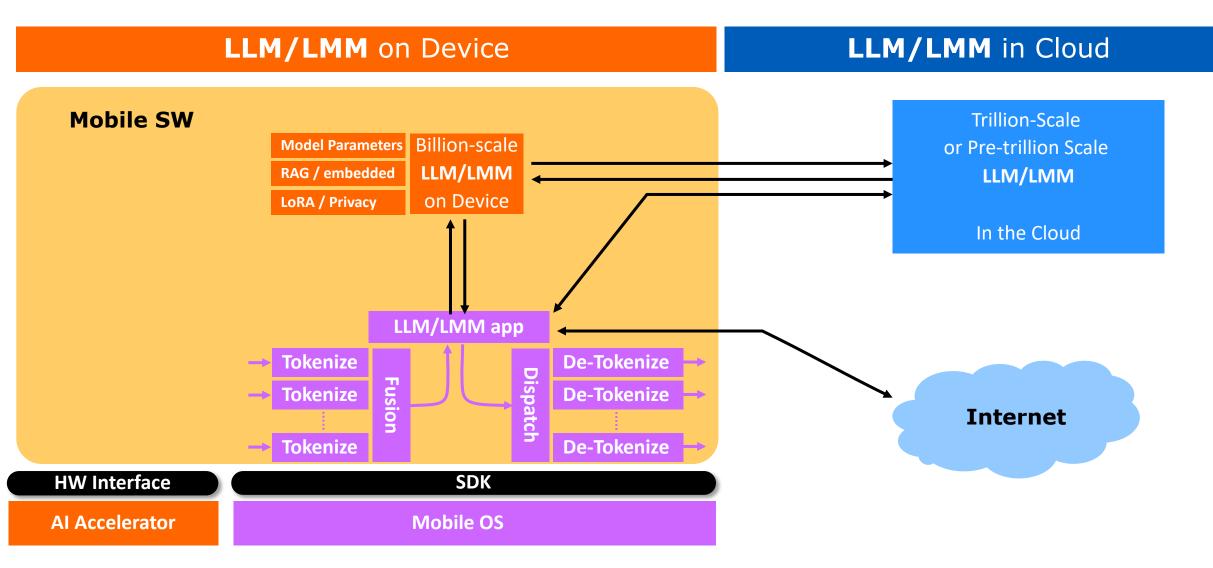
LLM/LMM – Thinking Fast, Deep Thinking and Swift Response



LLM /LMM on Device - Collaborate with Cloud and Mobile OS



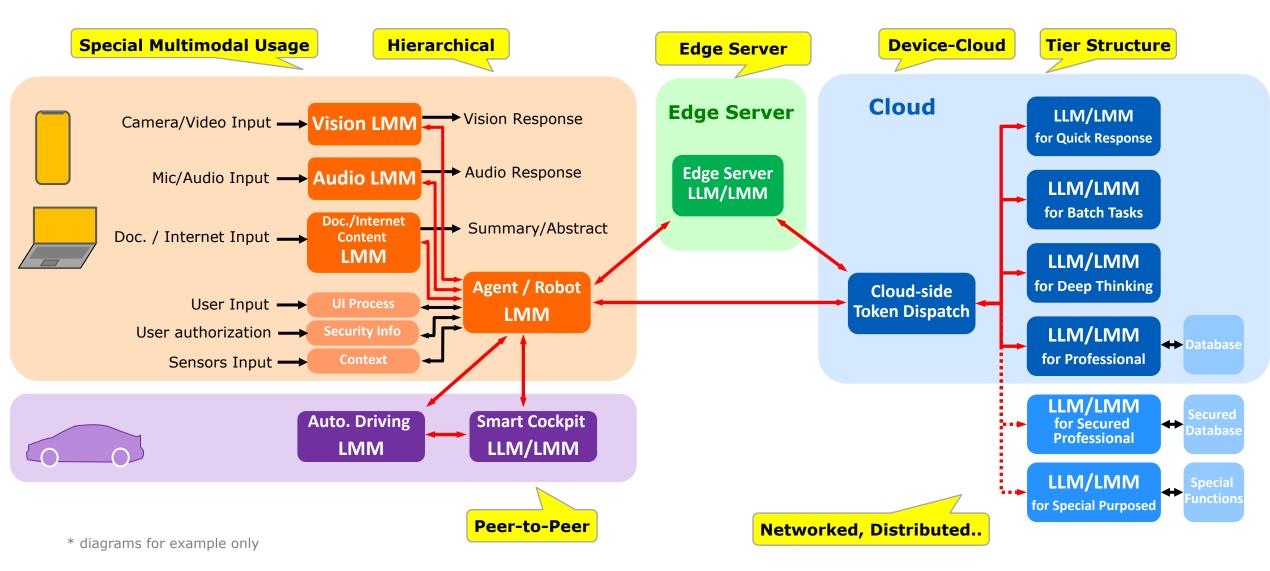
LLM /LMM as Mobile Software on Mobile Processor



LLM /LMM on Mobile Processor : Issues

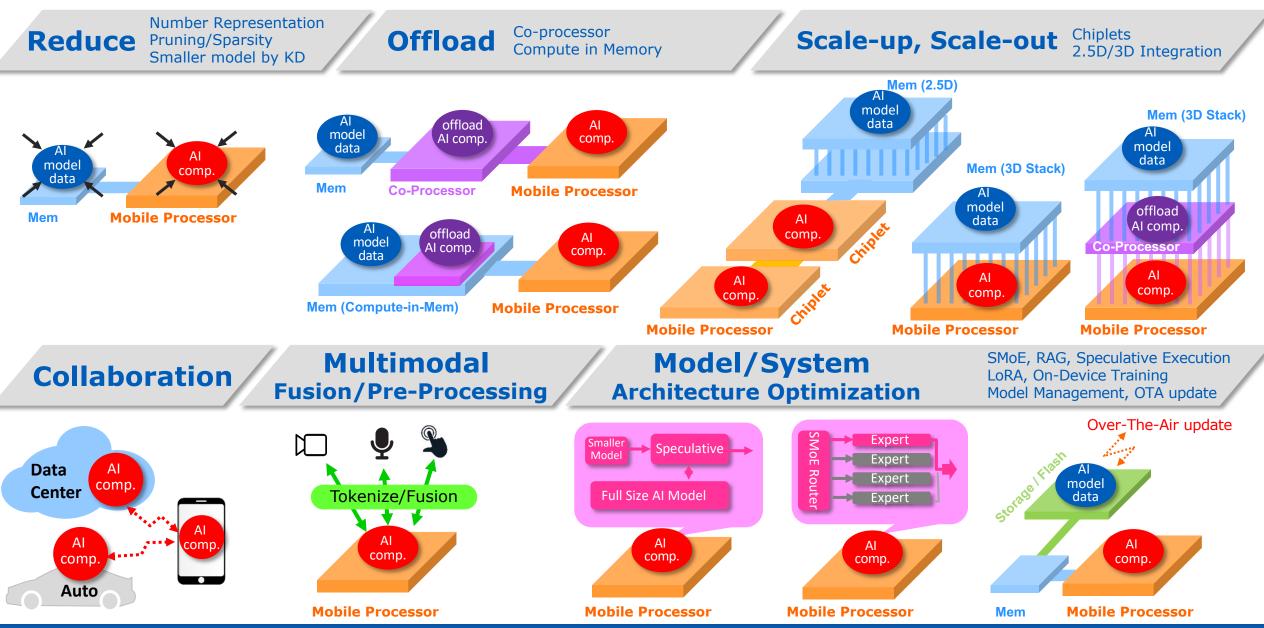
LLM/LMM in Cloud **LLM/LMM** on Device Avoid Hallucination **Channel Security** Mobile SW **Trillion-Scale** For LLM/LMM collaboration **Model Parameters** Billion-scale or Pre-trillion Scale Model and RAG database LLM/LMM **RAG / embedded** LLM/LMM **Over-The-Air Upgradeable** on Device LoRA / Privacy **On-Device Training** In the Cloud **Architecture Scalability** for User Privacy Multi-Task & **Multi-Thread Internet Agent Issues** Multimodal I/O **Avoid User Privacy Leakage** Permission, Payment, ... **Fusion and Priority** LLM/LMM app **Tokenize De-Tokenize** Disp Fus **HW/SW Interface** Tokenize **De-Tokenize Performance Issues** 0 Internet **Co-operation Tokenize De-Tokenize** with other Mobile APPs **HW Interface** SDK **Internet Security Power Efficiency & Avoid Prompt Injection Attack Mobile OS AI Accelerator Performance Optimization Anti-Spoof**

Collaboration among AI Models



Trends of Mobile Processor Design for LLM/LMM

REF: [1-8][31-42][44-53][55-56]



ISPD 2024 Computing Architecture for Large-Language Models (LLMs) and Large Multimodal Models (LMMs)

Trends of AI Computing for LLM/LMM - Continuous Evolution

AI Model Architecture

- Model Architecture Improvement (SMoE, RAG, Speculative Execution, LoRA, On-Device Learning..)
- Fundamental Model Architecture (Transformer, Mamba, RWKV..)
- **Collaboration among Models** (Device-Cloud, Multimodal Partition, Hierarchical, Networked, Distributed..)

Hardware Architecture

- 2.5D/3D Heterogeneous Integration, Chiplets, Interface (CoWoS, 3DSoC; PCIe, UCIe,.)
- Non-Von Neuman Architecture (Computing-in-Memory, Computing-Near-Memory, PIM,..)
- Memory Architecture and Emerging Memory (HBM, CXL,..; ReRAM, MRAM, PCM,..)
- Special Computing/Architecture Type (Neuromorphics, Analog Computing, Approximate computing, ..)

Device Types for Applications

- AI Smartphone, AI PC
- Portable AI Assistant (AI pin, Rabbit R1,..)
- AR/VR/XR, Spatial Computing
- Automotive, Robotics

REF: [1-8][31-42][44-53][55-58]

Conclusion

LLM/LMM to Shape Mobile Processor Design

- **<u>Higher Token Speed</u>**: More AI Accelerators (TOPS) , Memory Bandwidth, Memory Size,...
- Inference Efficiency : More Techniques to Improve LLM/LMM Inference on Devices
- AI Models Collaboration: Efficient Collaboration among AI Models in Different Devices & Clouds

LLM/LMM to Shape Mobile Device Applications

- UI by Natural Communication: Understanding Nuanced Expressions in Natural Language and Body Language
- AI Agent : Professional Agents for Device and Internet Interactions
- Deep Thinking Quality : Enhanced by Cloud-side LLMs and Networked/Distributed AI Models

□ AI Inference to Shape LLM/LMM Architecture

- **Optimized AI Model for Inference**: Smaller Model, Specific Architecture, Hardware-Software-Domain Co-design
- New Fundamental Model Architecture : New Algorithm and Structure for Higher Efficient Inference
- An Exciting Area with Profound Impact to Shape Next-Generation Mobile Processors. However, Breakthroughs in Domain-Specific Architecture and in Semiconductor Tech are Required!

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