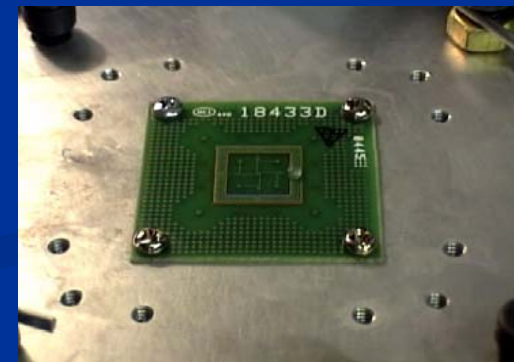
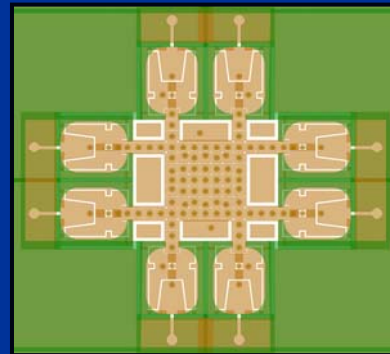
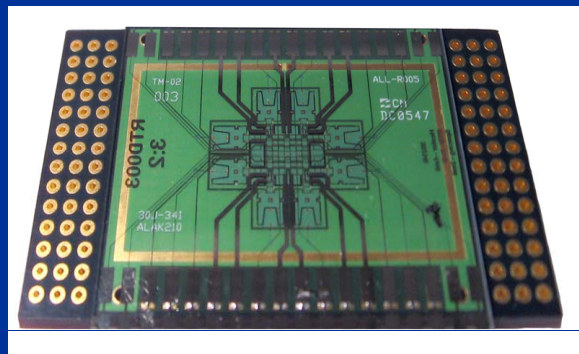
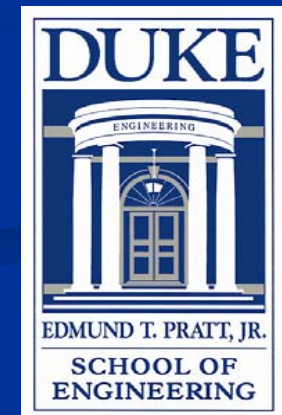


# Automated Design of Digital Microfluidic Lab-on-Chip under Pin-Count Constraints



**Krishnendu Chakrabarty**

Department of Electrical and Computer Engineering  
Duke University  
Durham, North Carolina  
USA



# Acknowledgments

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- Duke University's Microfluidics Research Lab (<http://www.ee.duke.edu/research/microfluidics/>)
- Advanced Liquid Logic (<http://www.liquid-logic.com/>): Start-up company spun out off Duke University's microfluidics research project



National Science Foundation  
WHERE DISCOVERIES BEGIN



Advanced Liquid Logic, Inc.  
nanoliter lab-on-a-chip powered by digital microfluidics

# Talk Outline

- **Motivation**
- **Technology overview**
- **Design of high-throughput pin-constrained lab-on-chip**
  - Array partitioning
  - Cross-referencing-based biochip
  - High-throughput droplet manipulation
- **Conclusions**

# Applications and Advantages of Lab-on-Chip

## Applications

- Point-of-care clinical diagnostics, newborn screening
- Environmental monitoring
- Massively-parallel DNA sequencing
- Automated drug discovery

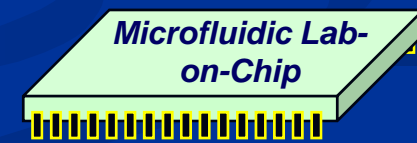
## Advantages

- Automated
- Small sample/reagent cost
- High sensitivity



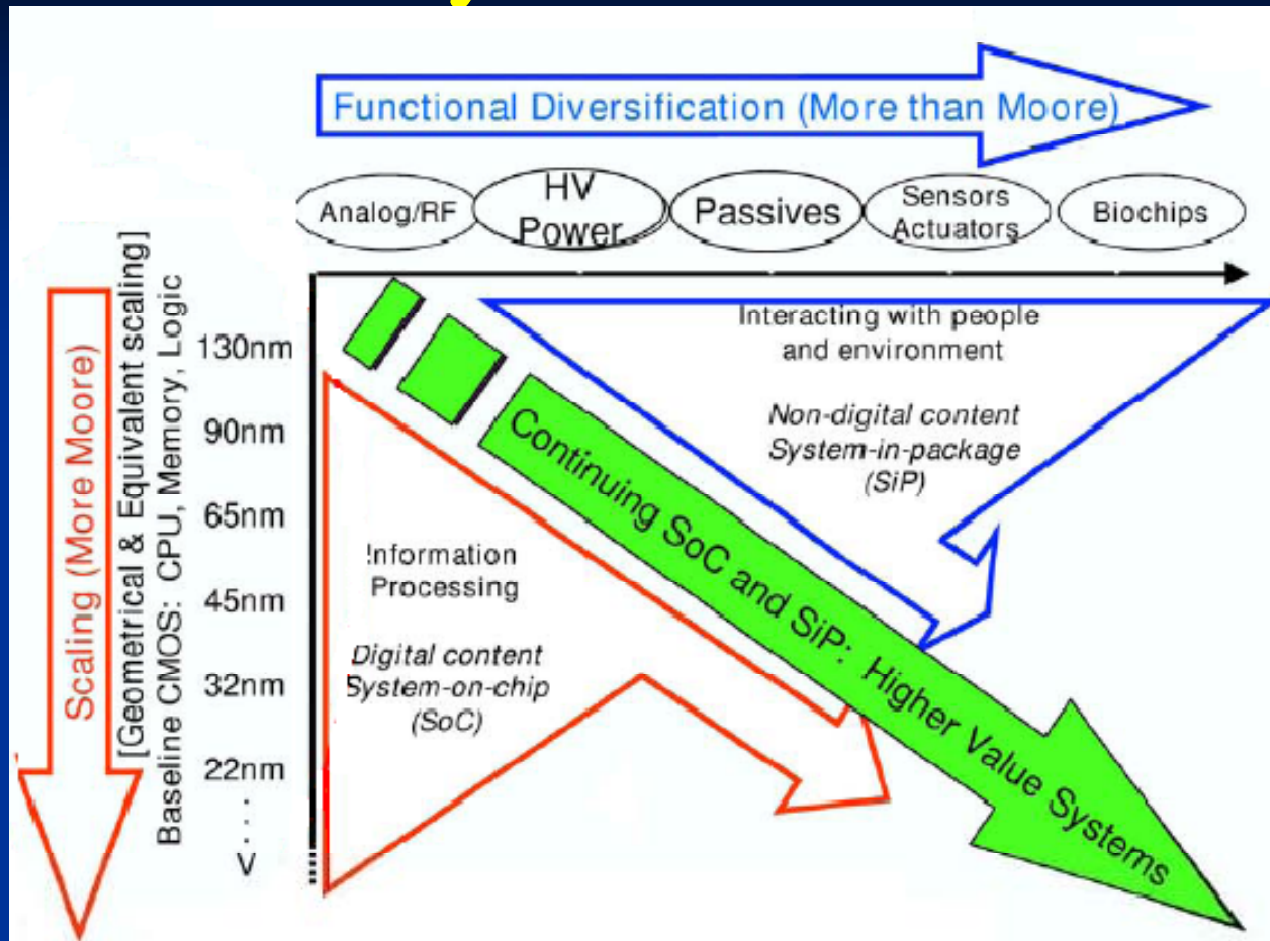
Conventional Biochemical Analyzer

*Shrink*



20nl sample

# Why Do We Care?



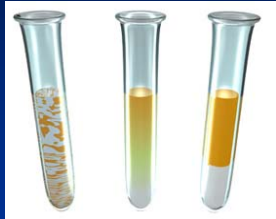
International Technology Roadmap for Semiconductors

System Driver  
for 2009:  
"Medical"

Final Draft 2007

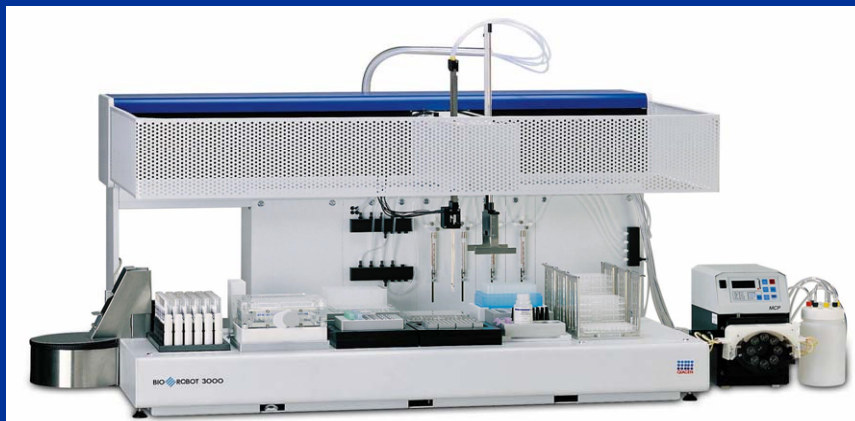
Intel Research Day 2007: Biochip prototype demonstrated for point-of-care diagnostics and lab testing

# Motivation for Microfluidics



Test tubes

- Automation
- Integration
- Miniaturization



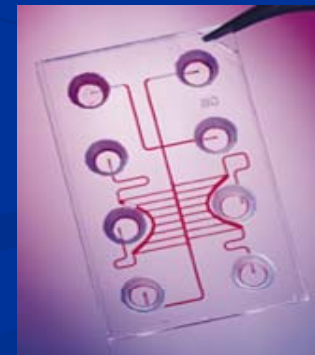
Robotics

- Automation
- Integration
- Miniaturization



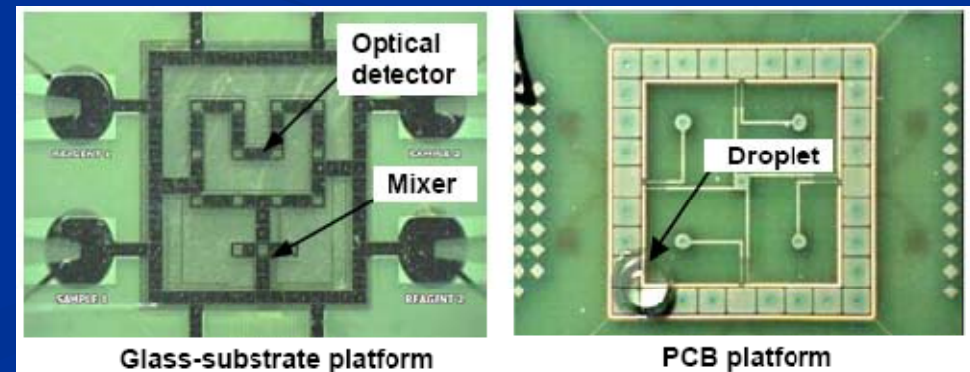
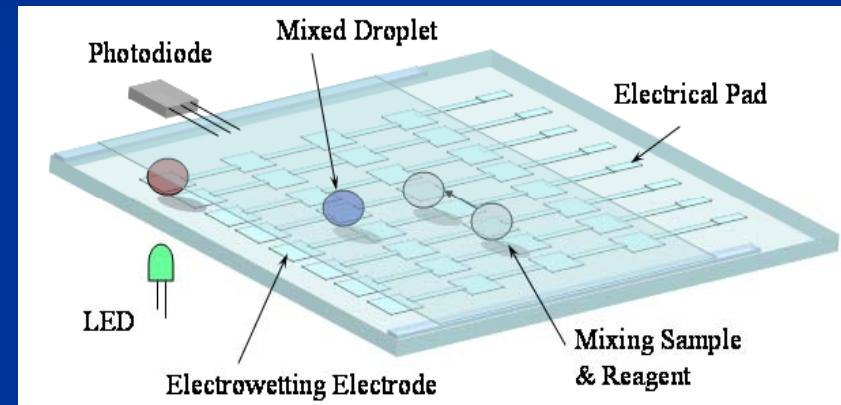
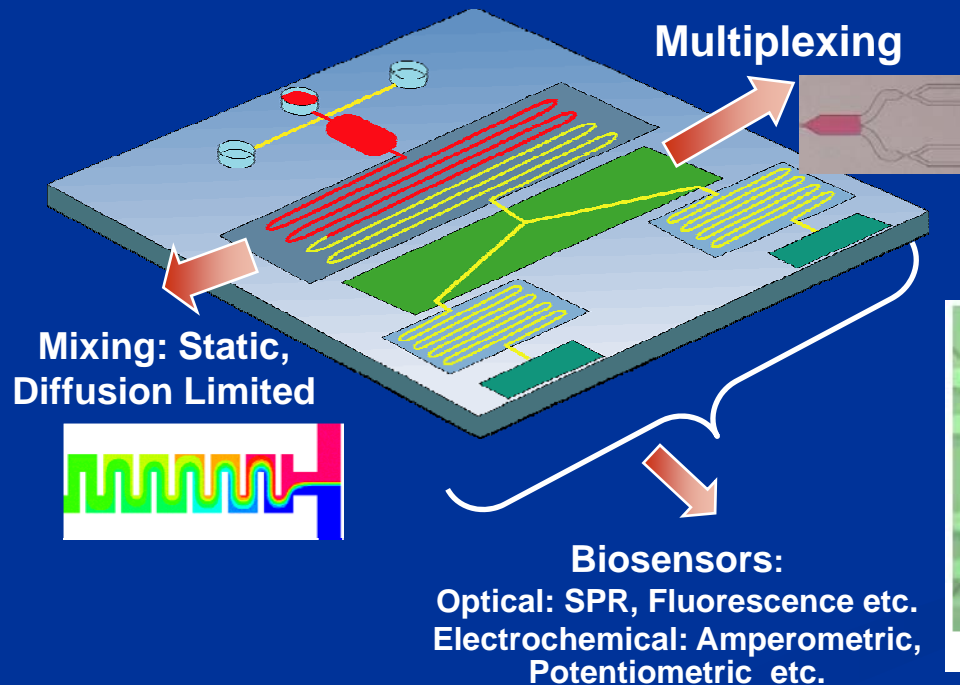
Microfluidics

- Automation
- Integration
- Miniaturization



# Microfluidics

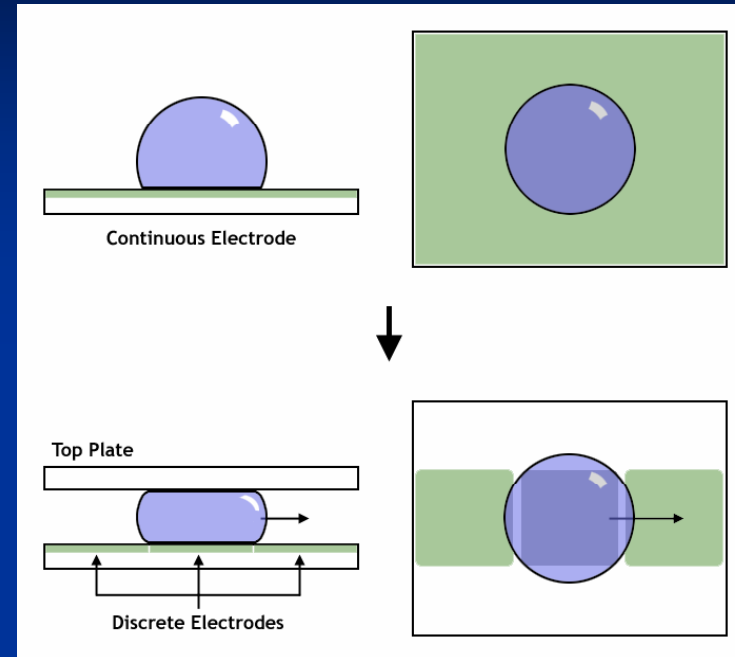
- Continuous-flow lab-on-chip: Permanently-etched microchannels, micropumps and microvalves, electrokinetics, etc.
- Digital microfluidic lab-on-chip: Manipulation of liquids as discrete droplets



# What is Digital Microfluidics?

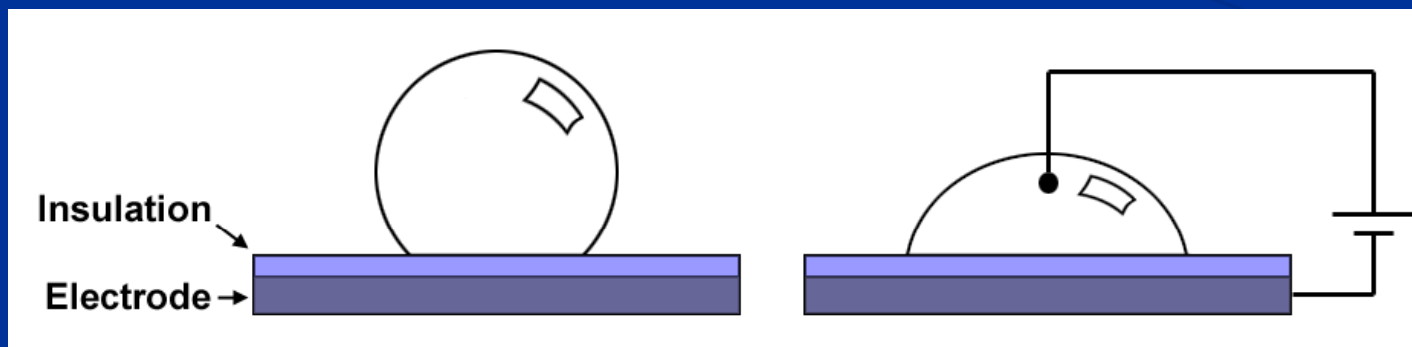
- Droplet actuation is achieved through an effect called *electrowetting*

— Electrical modulation of the solid-liquid interfacial tension

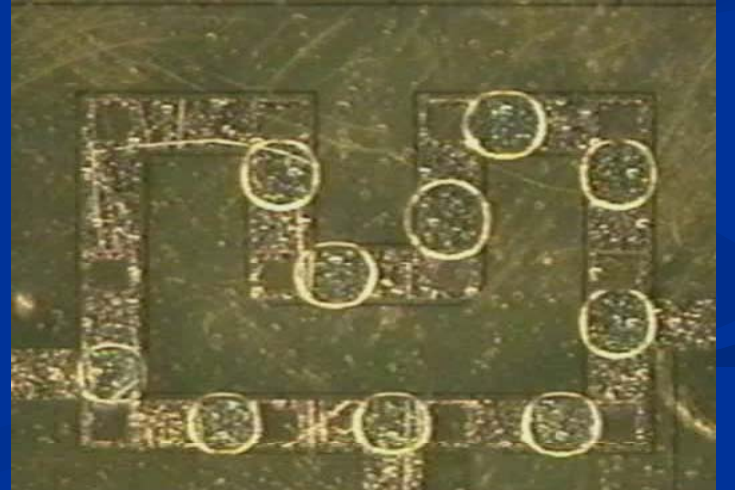
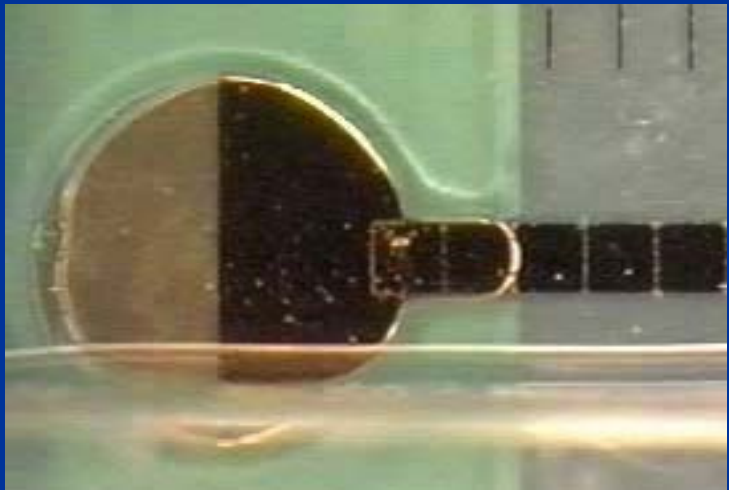


No Potential

Applied Potential

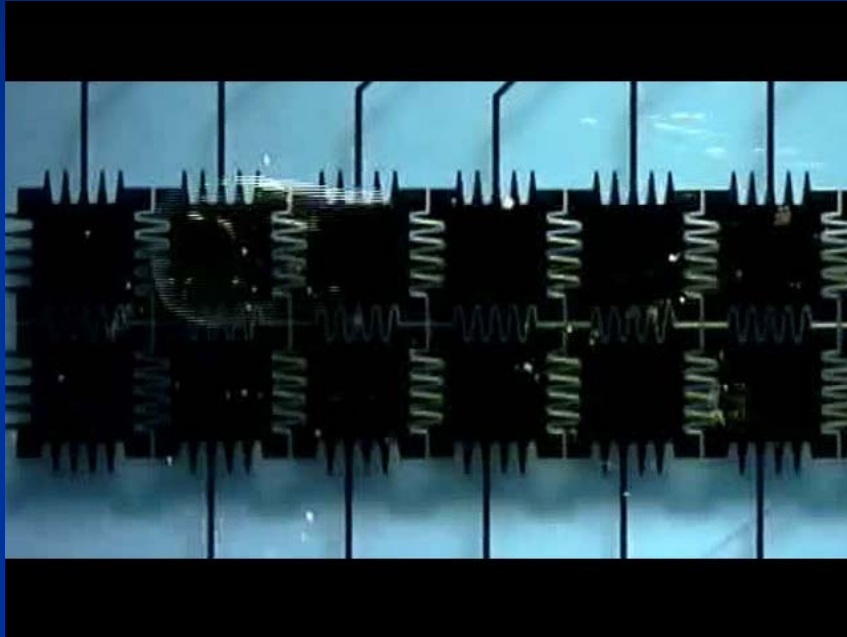


# Demonstrations



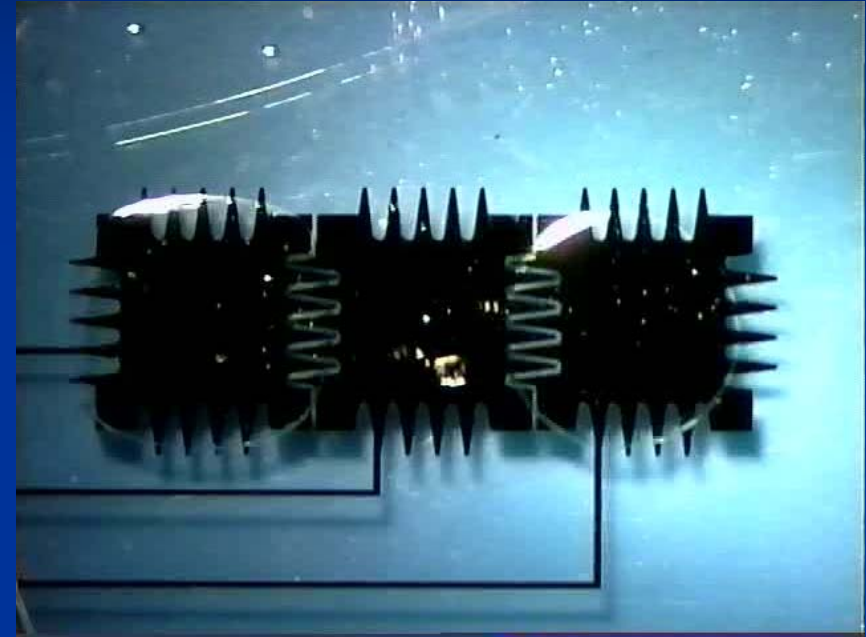
Video source: [www.ee.duke.edu/research/microfluidics](http://www.ee.duke.edu/research/microfluidics)

# Some Basic Operations



## Transport

25 cm/s flow rates, order of magnitude higher than continuous-flow methods



## Splitting/Merging

# Current Capabilities

## ■ Digital microfluidic lab-on-chip

TRANSPORT

DISPENSING

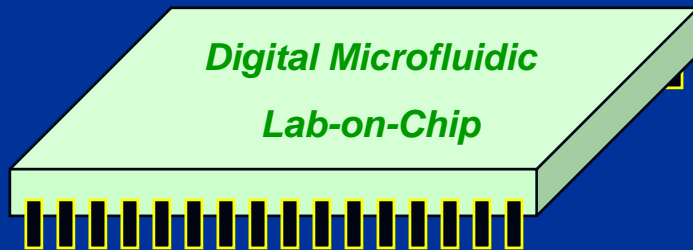
MIXERS

REACTORS

DETECTION

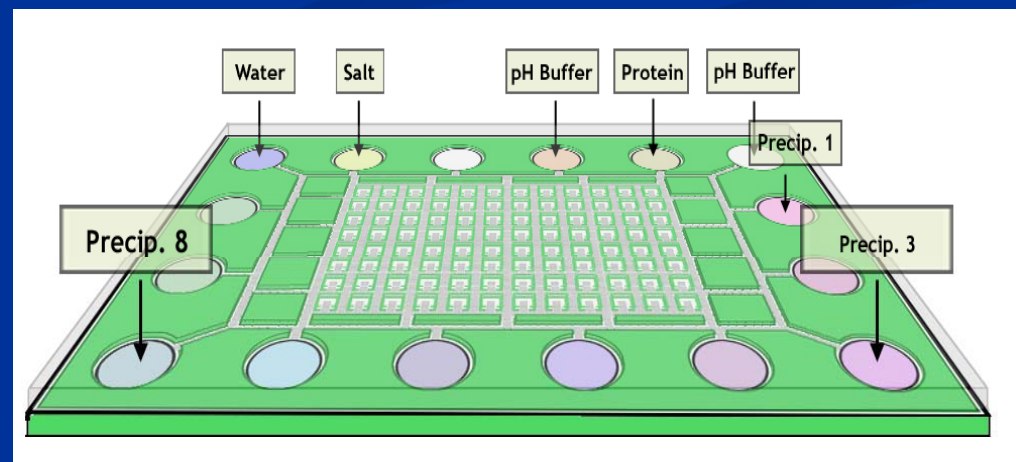
INTEGRATE

Digital Microfluidic  
Lab-on-Chip



Protein crystallization chip  
(under development)

- Basic microfluidic functions (transport, splitting, merging, and mixing) have already been demonstrated on a 2-D array
- Highly reconfigurable system



# Emerging Trends and Needs for Lab-on-Chip

## ■ High throughput

- DNA sequencing,  $10^6$  base pairs
- Protein crystallization,  $10^3$  candidate conditions

## ■ Low cost

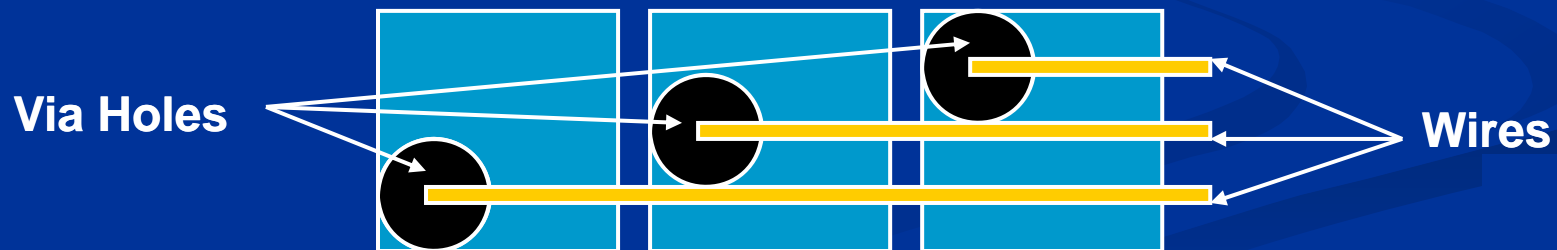
- Disposable, low-cost, less than \$1/chip
- PCB design
  - Rapid prototyping and inexpensive mass-fabrication
  - Copper layer for electrodes (coplanar grounding rails)
  - Solder mask for insulator
  - Teflon AF coating for hydrophobicity
- Disposable PCB device plugged into controller circuit board, programmed and powered with USB port

# Electrode-Addressing Problem

## Direct Addressing:

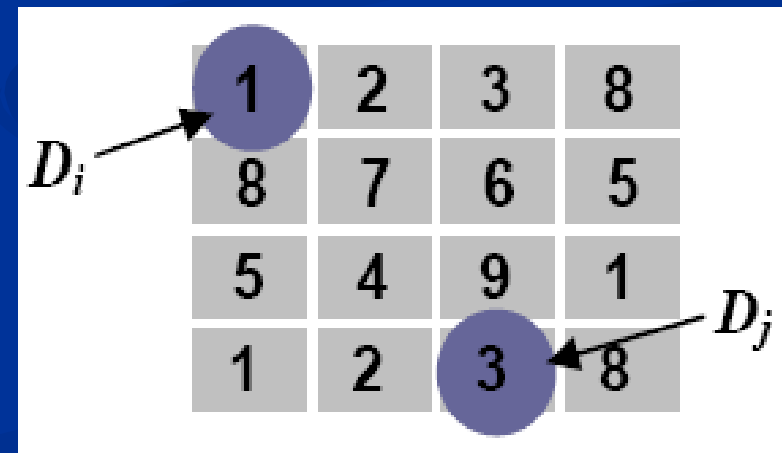
- Each electrode connected to an independent pin
- For larger arrays (e.g.,  $> 100 \times 100$  electrodes)
  - Too many control pins  $\rightarrow$  high fabrication cost
  - Complicated wiring, too many PCB layers, high cost

PCB design: 250  $\mu\text{m}$  via hole, 500  $\mu\text{m}$  x 500  $\mu\text{m}$  electrode



# Solution Based on Array Partitioning

- Pin-constrained array design
  - **Advantage:** Reduce number of independent pins for  $n \times m$  array from  $n \times m$  to  $k \leq n \times m$ 
    - $k = 5$  is fewest # of control pins to control single droplet
  - **Disadvantage:** Potential for unintentional interference between multiple droplets: no way to concurrently move  $D_i$  to position (1,2) and  $D_j$  to position (4,4)
- Solution
  - Single droplet: Addressing each electrode and its neighbors with distinct pins
  - Multiple droplets: Partition the chip
- Need for stall cycles?



# Partitioning for Pin-Constrained Designs

## ■ *Droplet Trace*

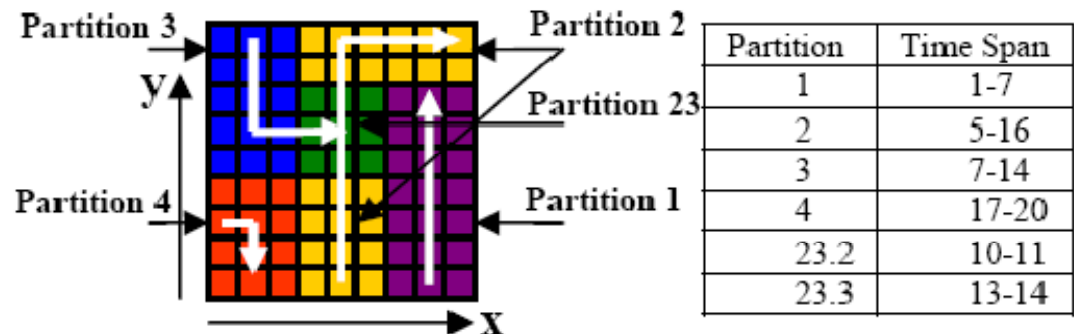
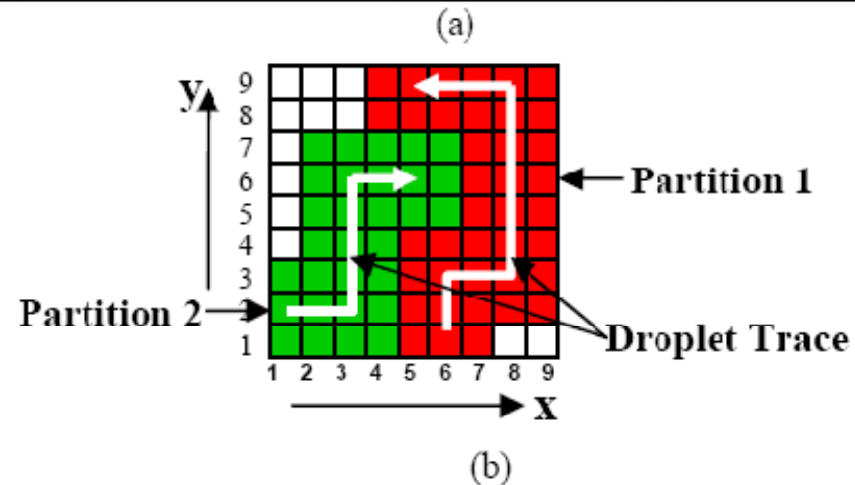
- all the cells traversed by a droplet in its lifetime

## ■ Scheduling and placement information needed

## ■ Partitioning rules

- non-overlapping partitions
- spatially overlapping partitions
- temporally overlapping partitions

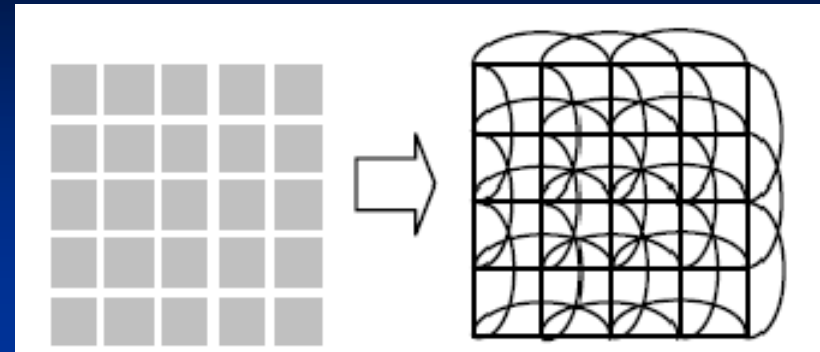
	Detector1(x,y)	Detector2(x,y)	Detector3(x,y)
Droplet 1	(8, 3)	(8, 9)	(5, 9)
Droplet 2	(3, 2)	(3, 6)	(5, 6)



# Pin Assignment in Each Partition

- Goal

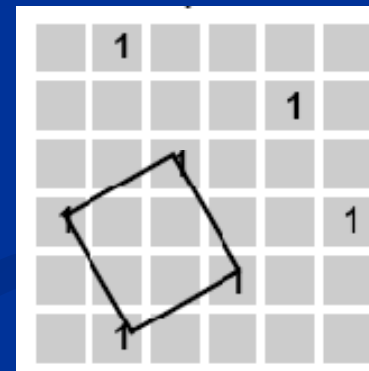
- Addressing each electrode and its neighbors with distinct pins



- Problem formulation

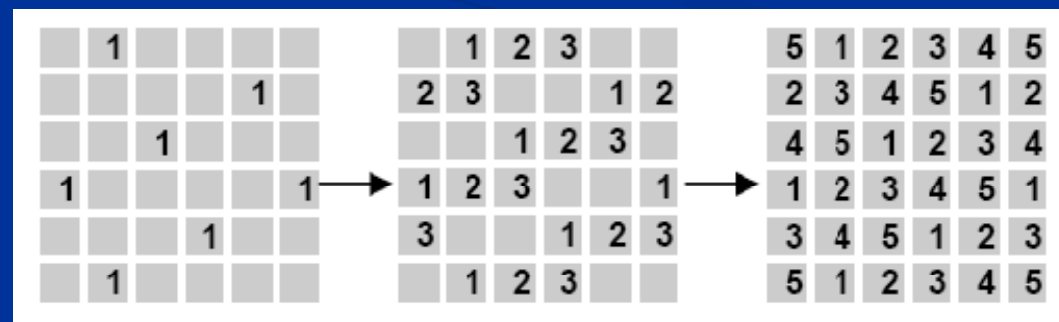
- Vertex coloring problem from graph theory

*5 pins (colors) are sufficient for each partition!*



- *Connect-5* algorithm

- Bagua structure
- Tiling the Bagua structure





# Cross-Referencing-Based Design

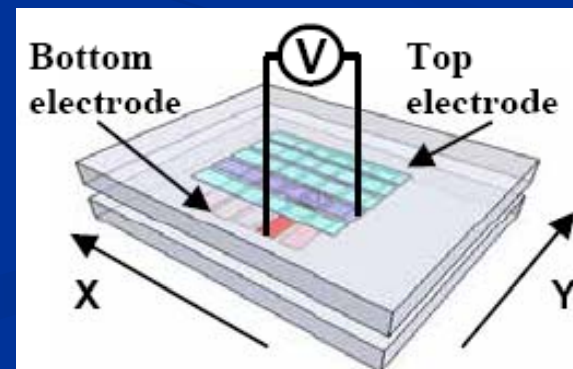
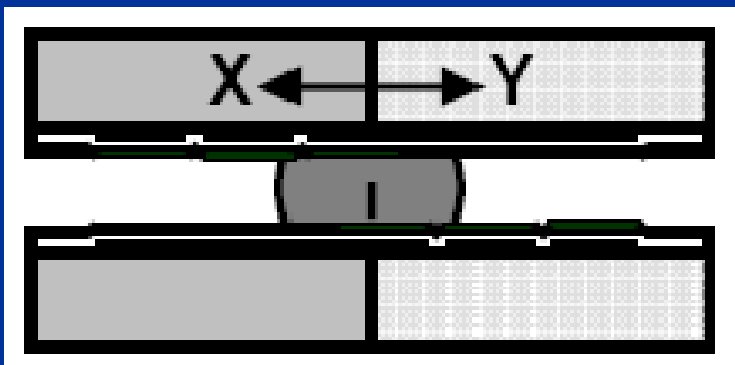
- Orthogonally placed pins on top and bottom plates

## Advantage

$k = n \times m \rightarrow n + m$  for a  $n$  by  $m$  microfluidic array

## Disadvantage

Suffers from *electrode interference*

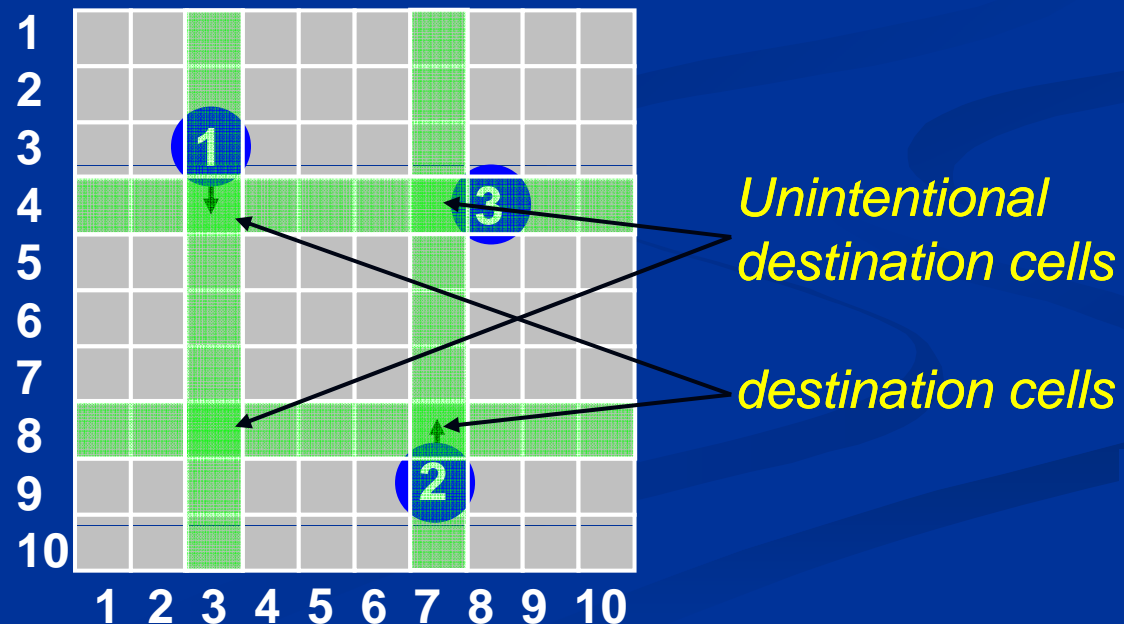


# Electrode Interference

- **Unintentional Electrode Actuation**

Selected column and row pins may intersect at multiple electrodes

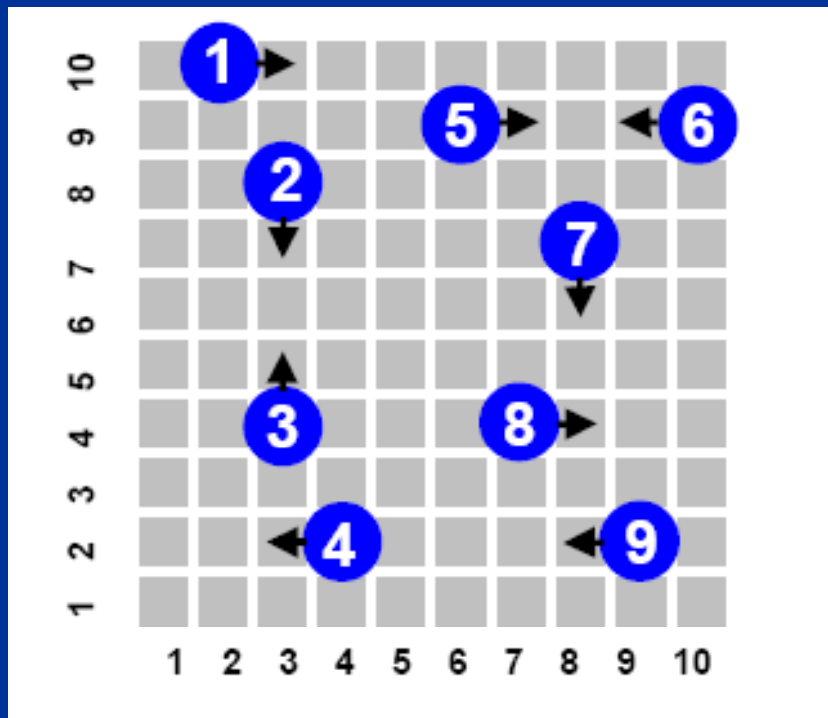
- **Unintentional Droplet Manipulation**



# Efficient Droplet Manipulation Method

## ■ Goal

- Improve droplet manipulation concurrency on cross-referencing-based biochips.

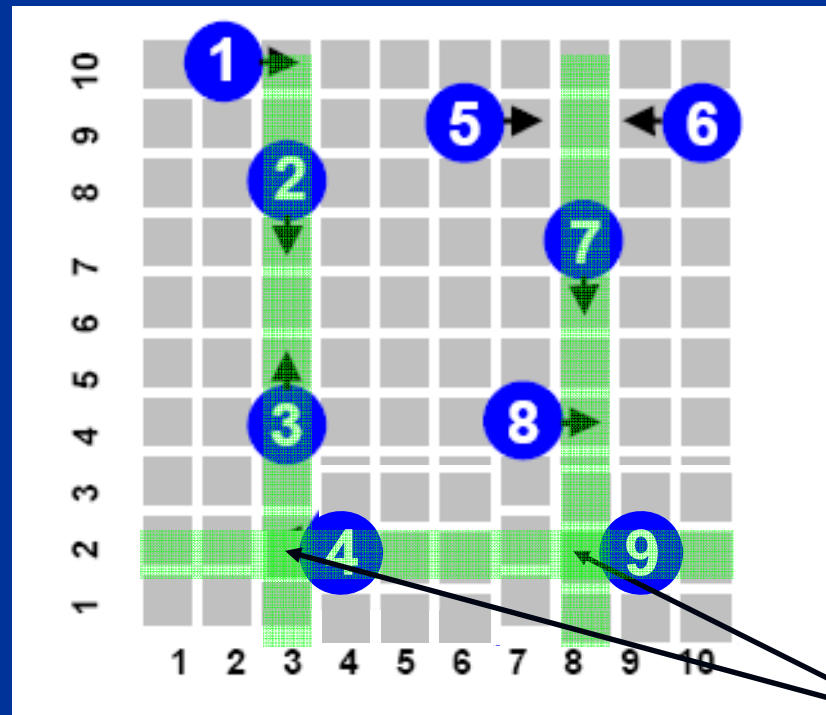


*9 steps needed if moving one droplet at a time (Too slow)*

# Efficient Droplet Manipulation Method

## ■ Observation

- Droplet manipulations whose *destination cells* belongs to the same column/row can be carried out without electrode interferences.



*destination cells*

# Efficient Droplet Manipulation Method

## ■ Methodology

- Group droplet manipulations according to their *destination cells*
- All manipulations in a group can be executed simultaneously

*The goal is to find the optimal grouping plan which results in the minimum number of groups.*

# Efficient Droplet Manipulation Method

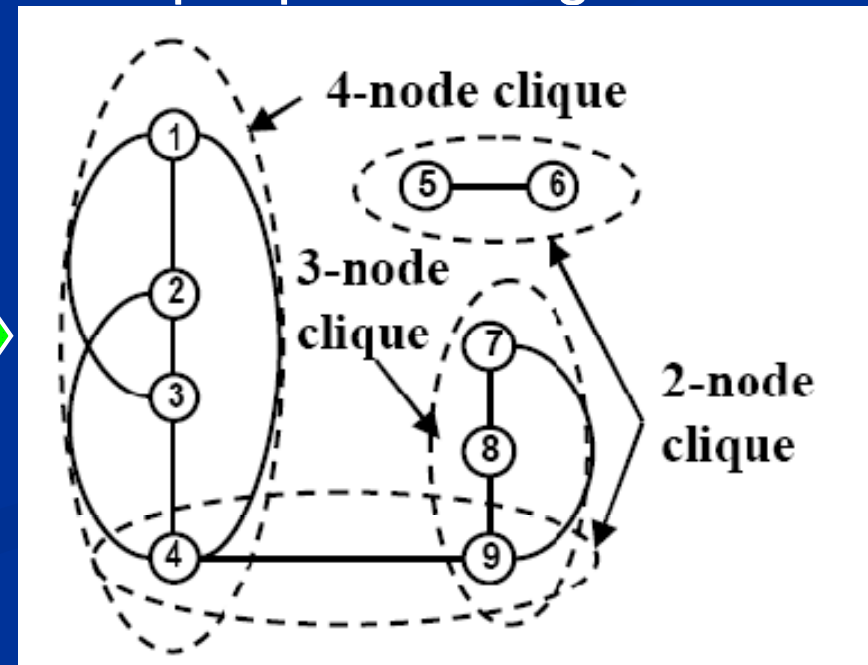
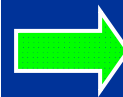
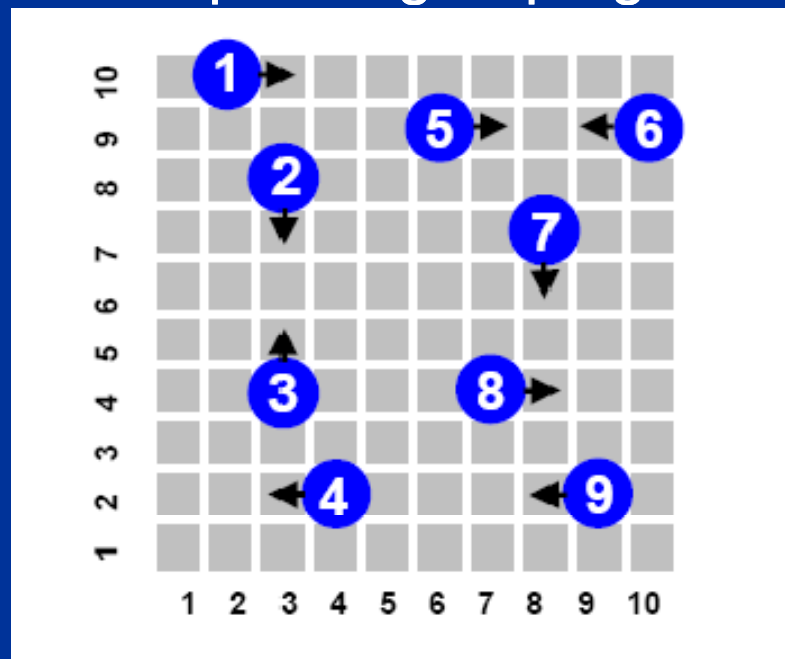
## ■ Problem formulation

Destination cells  $\rightarrow$  Nodes

Destination cells in one column/row  $\rightarrow$  a Clique

Grouping  $\rightarrow$  Clique partitioning

Optimal grouping  $\rightarrow$  Minimal clique-partitioning



# Broadcast Electrode-Addressing

## ■ Observation

### “Don’t-Cares” in Electrode-Actuation Sequences

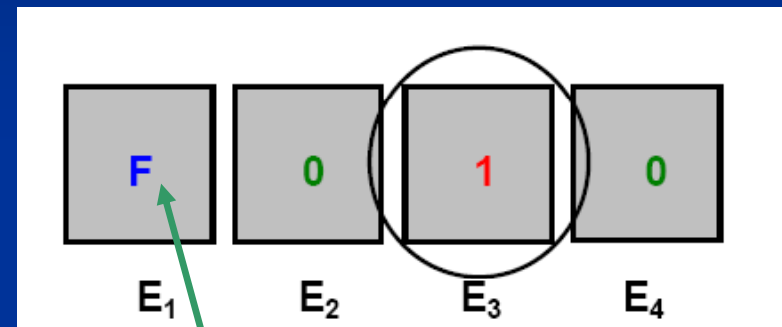
Electrode control inputs: 3 values

“1” -- activated

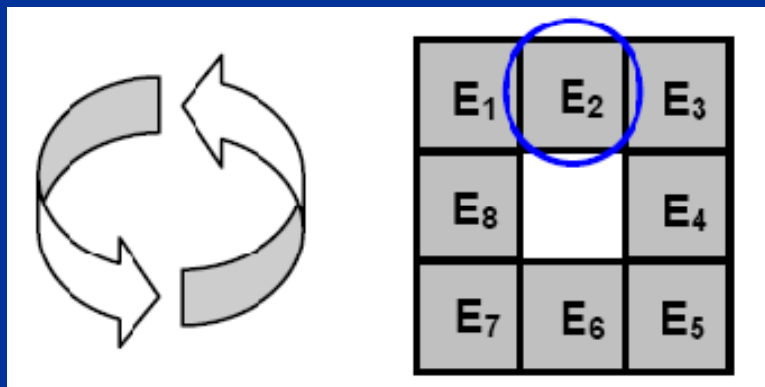
“0” -- deactivated

“x” -- can be either “1” or “0”

*Therefore, activation sequences can be combined by interpreting “x”*



*Floating electrode*



**Example: A droplet routed counterclockwise on a loop of electrodes**

Electrode	1	2	3	4	5	6	7	8
Activation Sequence	0	1	0	0	X	X	X	X
	1	0	0	X	X	X	X	0
	0	0	X	X	X	X	0	1
	0	X	X	X	X	0	1	0
	X	X	X	X	0	1	0	0
	X	X	X	0	1	0	0	X
	X	X	0	1	0	0	X	X
	X	0	1	0	0	X	X	X

**Corresponding electrode activation sequences**

# Electrode Addressing Based on Clique Partitioning in Graphs

## ■ Idea

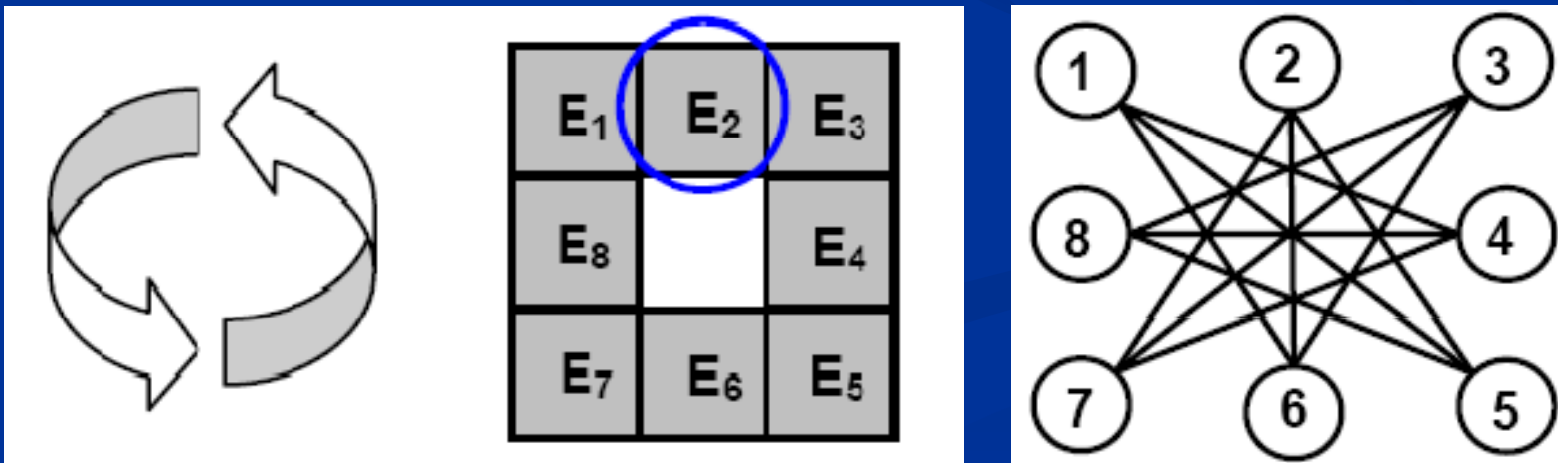
- Combining compatible sequences to reduce # of control pins

## ■ Clique-partitioning-based method

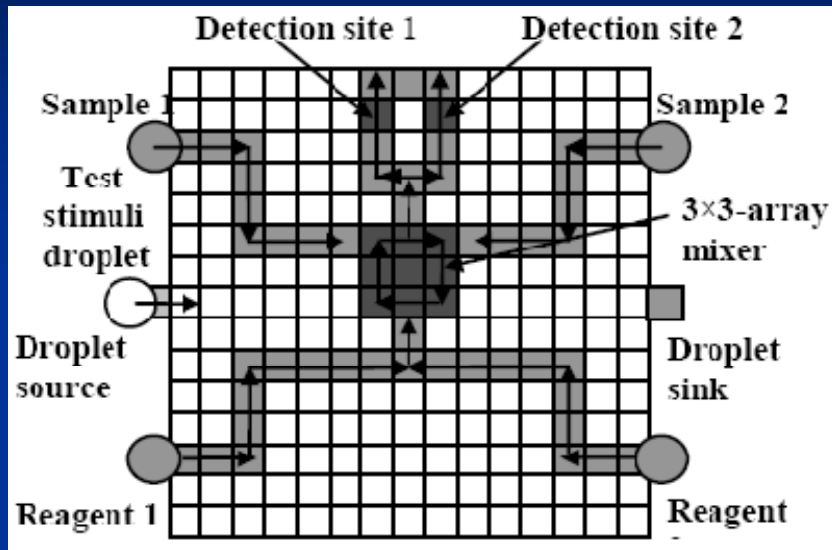
Electrodes → Nodes

Electrodes with compatible activation sequences → a clique

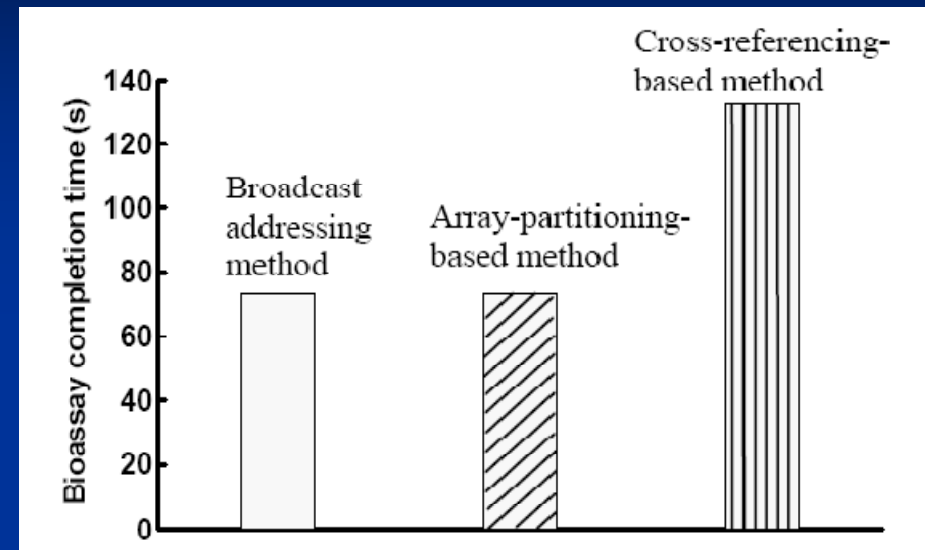
Optimal combination → Minimal clique-partitioning



# Addressing Results



A biochip target execution of a multiplexed assay



Comparison of bioassay completion time using different addressing methods

Addressing methods	Broadcast addressing	Array-partitioning-based method	Cross-referencing-based method
# of control pins	25	35	30

# Conclusions

- High concurrency can be achieved on pin-constrained lab-on-chip using a number of methods
  - Partitioning of the array based on droplet-movement patterns
  - Grouping of droplet movements based on clique partitioning
  - Exploiting flexibility in electrode-actuation sequences
- Array partitioning:
  - Specific to target application, number of pins determined such that there is no impact on assay completion time
- Clique partitioning in cross referencing:
  - Independent of target application, number of pins is fixed, and goal is to minimize impact on assay completion time
- Broadcast addressing:
  - Specific to target application, number of pins determined such that there is no impact on assay completion time
- Growing interest and ongoing work in CAD for digital microfluidic lab-on-chip: University of Texas (Austin), National Taiwan University, Penn State University, Rennselaer Polytechnic University, etc.