

PushPull: Short Path Padding for Timing Error Resilient Circuits

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Introduction

Problem Formulation

Algorithm - PushPull

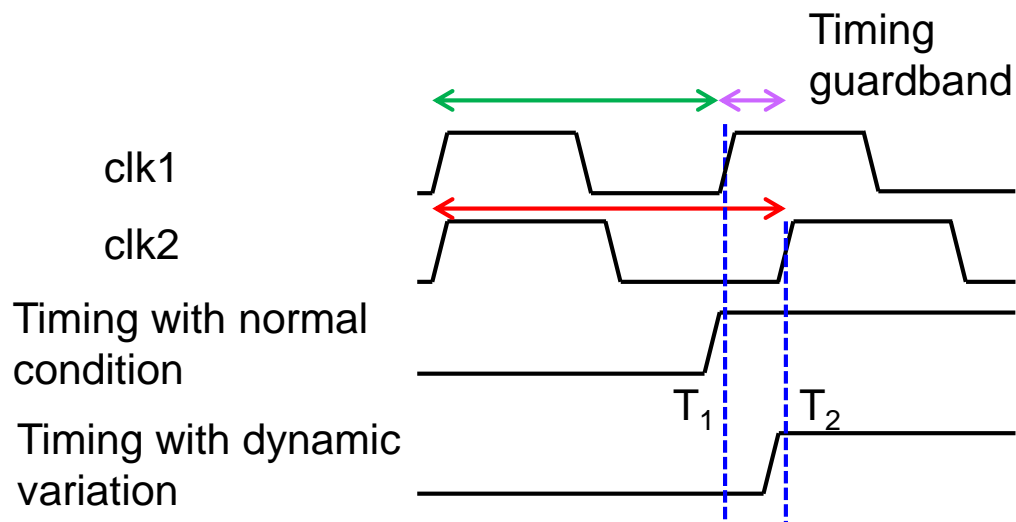
Experimental Results

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Introduction

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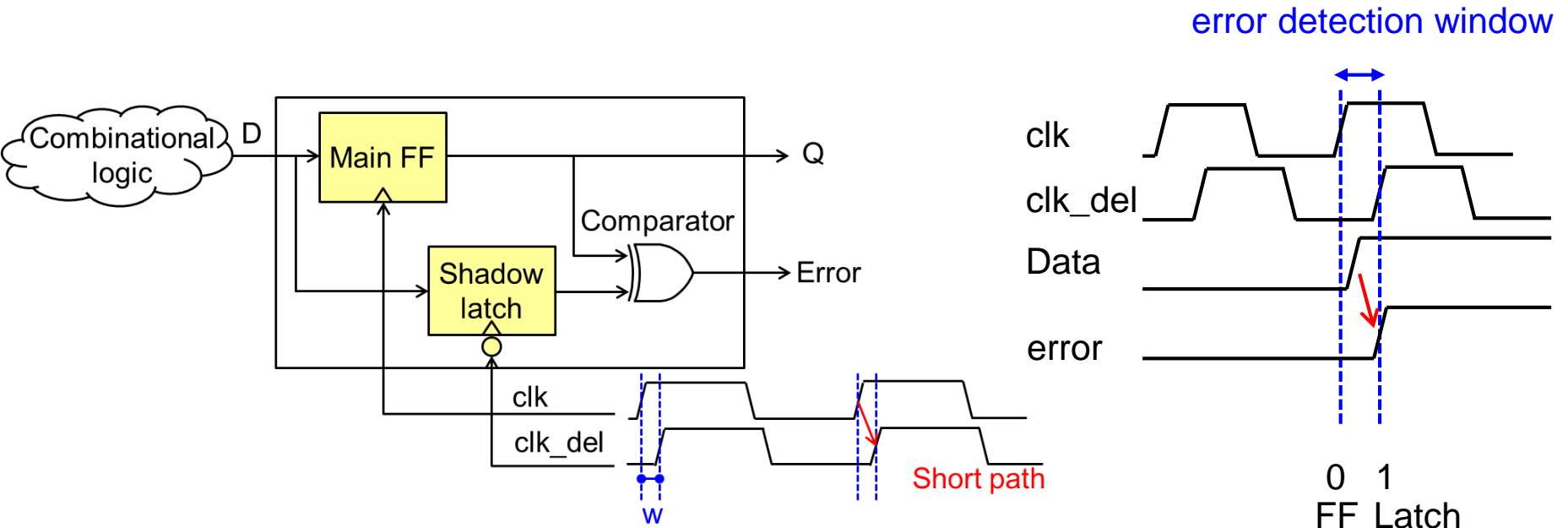
- **Timing characterization is difficult due to a wide range of dynamic variations**
 - ▣ Supply voltage droops, process variations, etc.
- **A timing guardband is reserved to ensure correct functionality**
 - ▣ Degrade circuit performance, i.e., limit the clock frequency



Resilient Circuit

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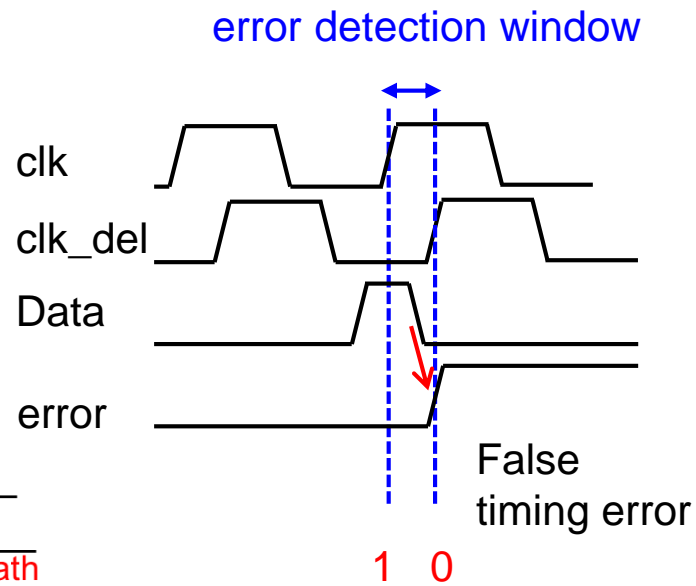
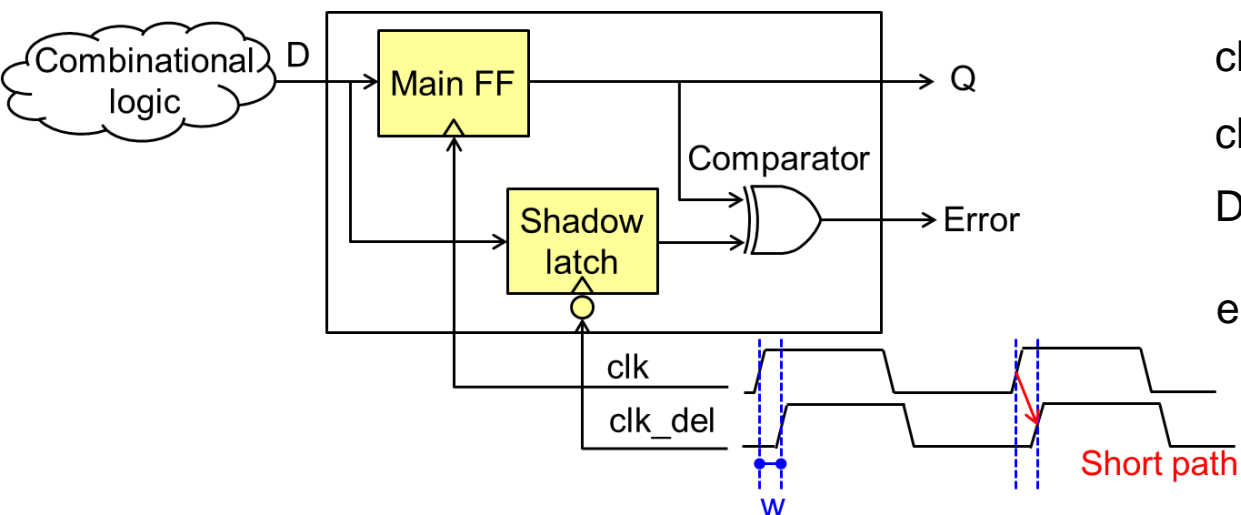
- **Eliminate the guardband by error detection and correction**
 - ▣ Ex: Razor flip-flop (one error-detection circuit)
 - ▣ Correction through instruction replay
 - ▣ Cons: **short path issue**



Short Path Issue

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- ❑ **Short paths should exceed the error detection window**
 - ❑ Otherwise, may detect false timing errors
- ❑ **Require a significant hold time margin for short paths**
- ❑ **Focus on short path padding in this paper**

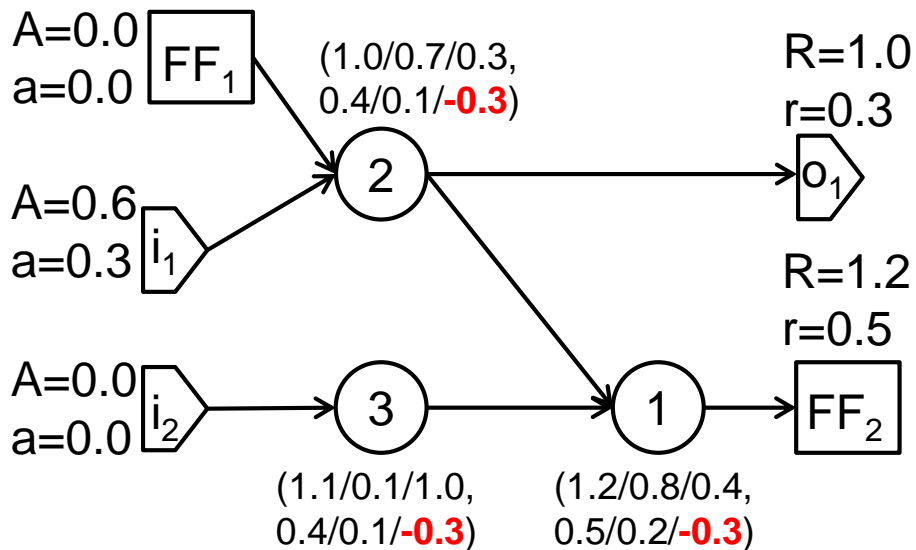


Previous Work

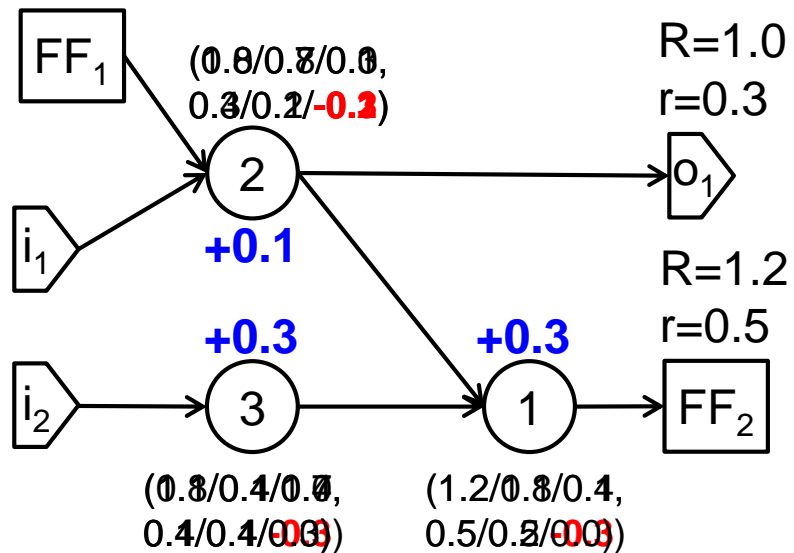
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- **Determine the padding delay path by path**
 - Combine with clock skew scheduling to minimize the clock period at logic synthesis stage
 - J.P. Fishburn, IEEE TC, 1990
 - R.B. Deokar and S.S. Sapatnekar, ISCAS, 1994
 - S.H. Huang et al., DAC, 2007
- **Determine the gate/wire to insert padding delay**
 - Solve by linear programming
 - N. V. Shenoy et al., ICCAD, 1993
 - Heuristics
 - Pad the gate with the largest setup slack
 - US Patent 6,990,646,2006 and 7,278,126,2007
 - Pad the gate passed by most hold violating paths
 - Y. Liu et al., DAC, 2011

Short Path Padding Example

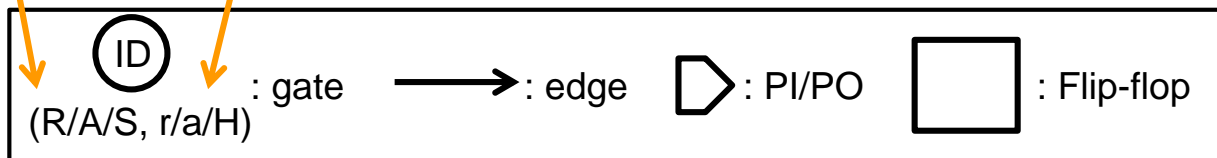


The largest setup slack



Setup Hold

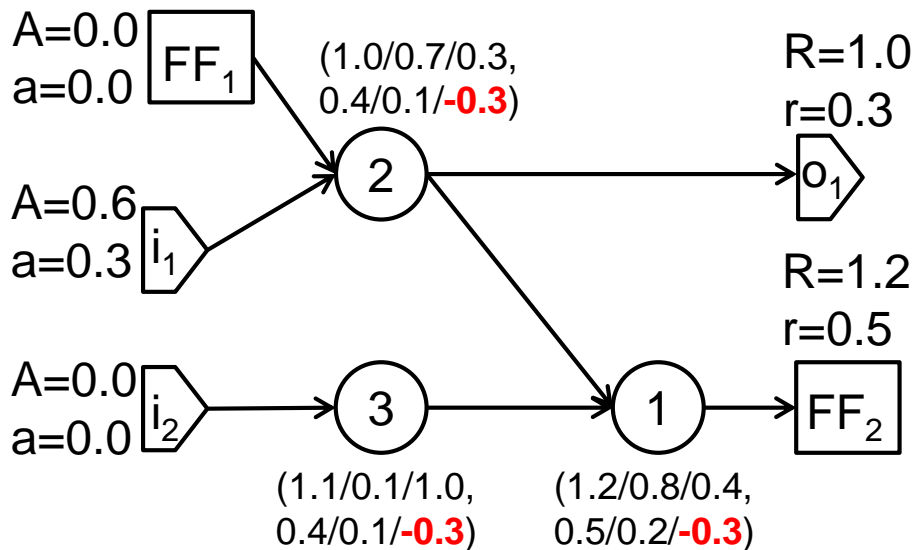
Legend:



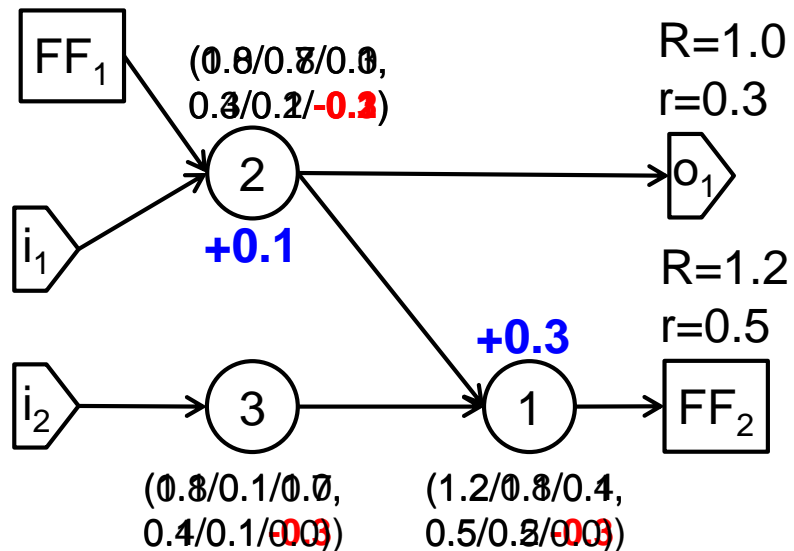
Unfix

ID	1	2	3
Delay	0.1	0.1	0.1

Short Path Padding Example (cont'd)

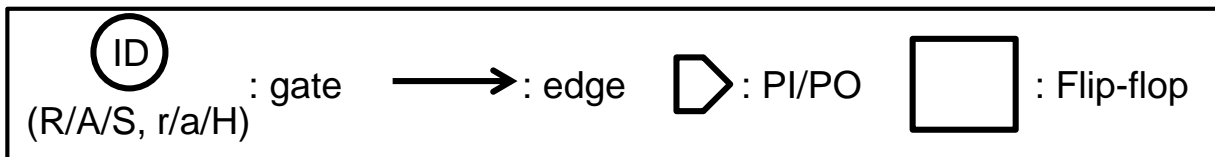


The most hold violating path



Unfix

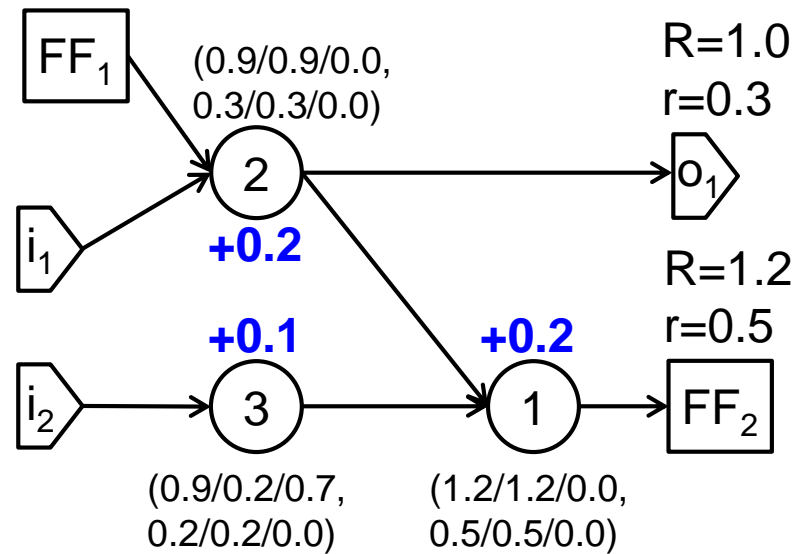
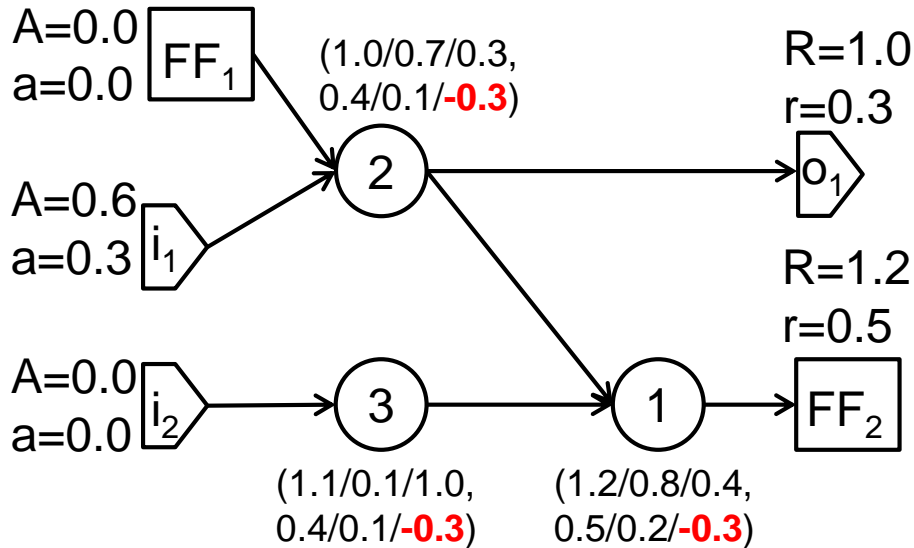
Legend:



ID	1	2	3
Delay	0.1	0.1	0.1

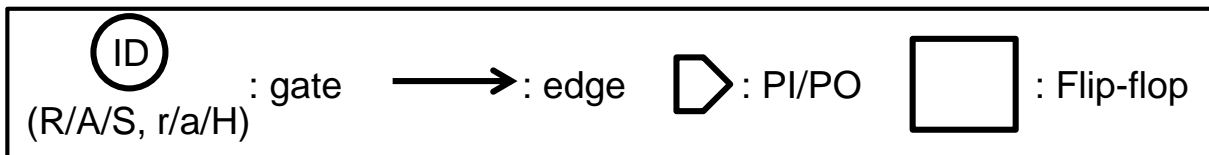
Short Path Padding Example (cont'd)

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Optimal padding delay = 0.5

Legend:



ID	1	2	3
Delay	0.1	0.1	0.1

Our Contributions

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- **Find the padding values and locations with a **global view****
 - Compute the fanout padding flexibility of each gate
- **Realize delay padding at the **post-layout** stage**
 - Coarse-grained delay padding: by spare cells
 - Fine-grained delay padding: by dummy metal

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Problem Formulation

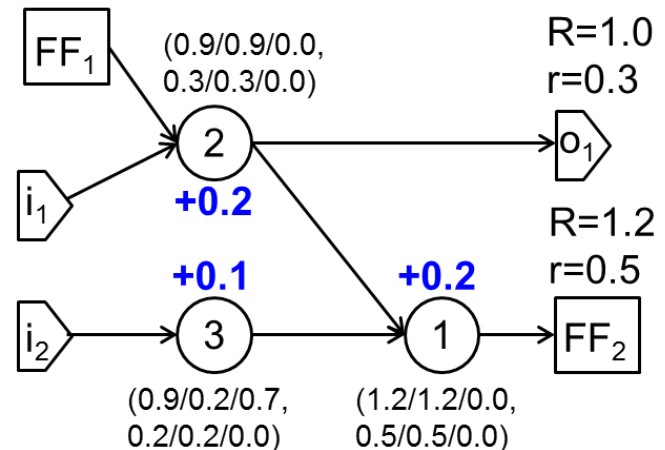
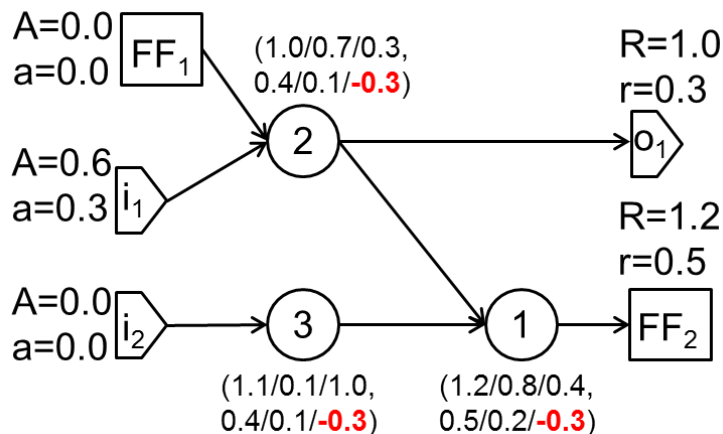
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Given

- Placed and routed resilient design
- Cell library
- Spare cells and dummy metal information
- Target clock period and error detection window

Goal

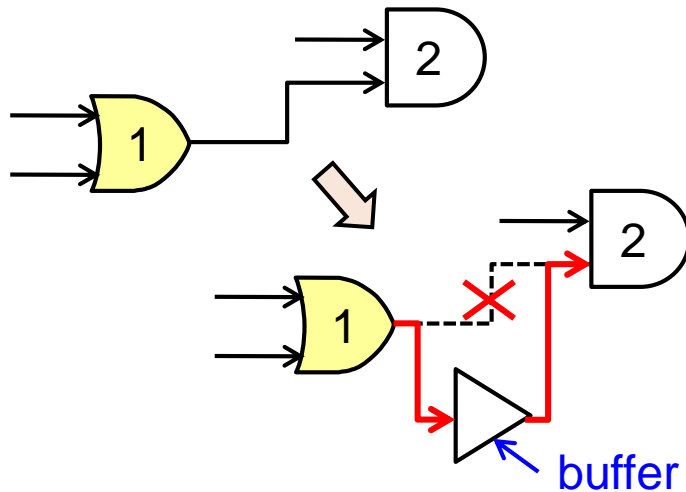
- Pad short paths
- Satisfy Setup/hold timing constraints
- Minimize the padding overhead



Delay Padding

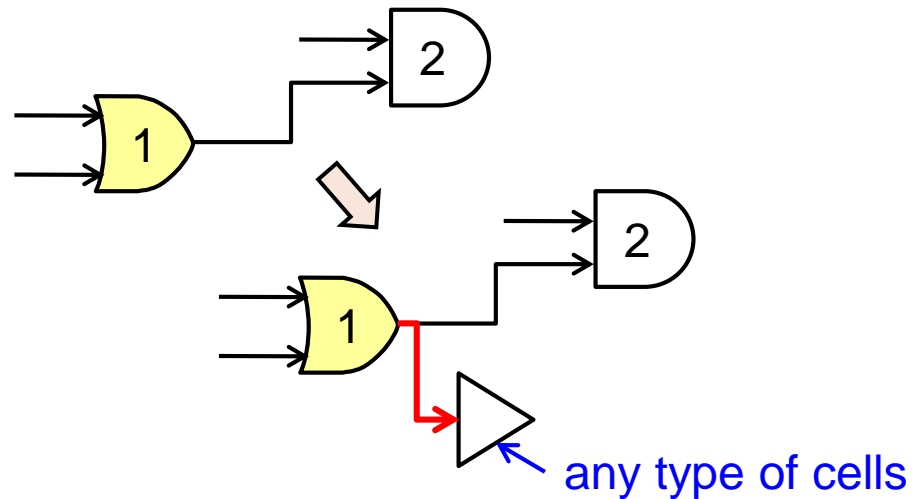
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- Lengthen short paths by **buffer insertion** and **extra capacitance hook-up**



Buffer insertion

Padding wire



Extra cap hook-up

Padding gate

Outline

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Problem Formulation

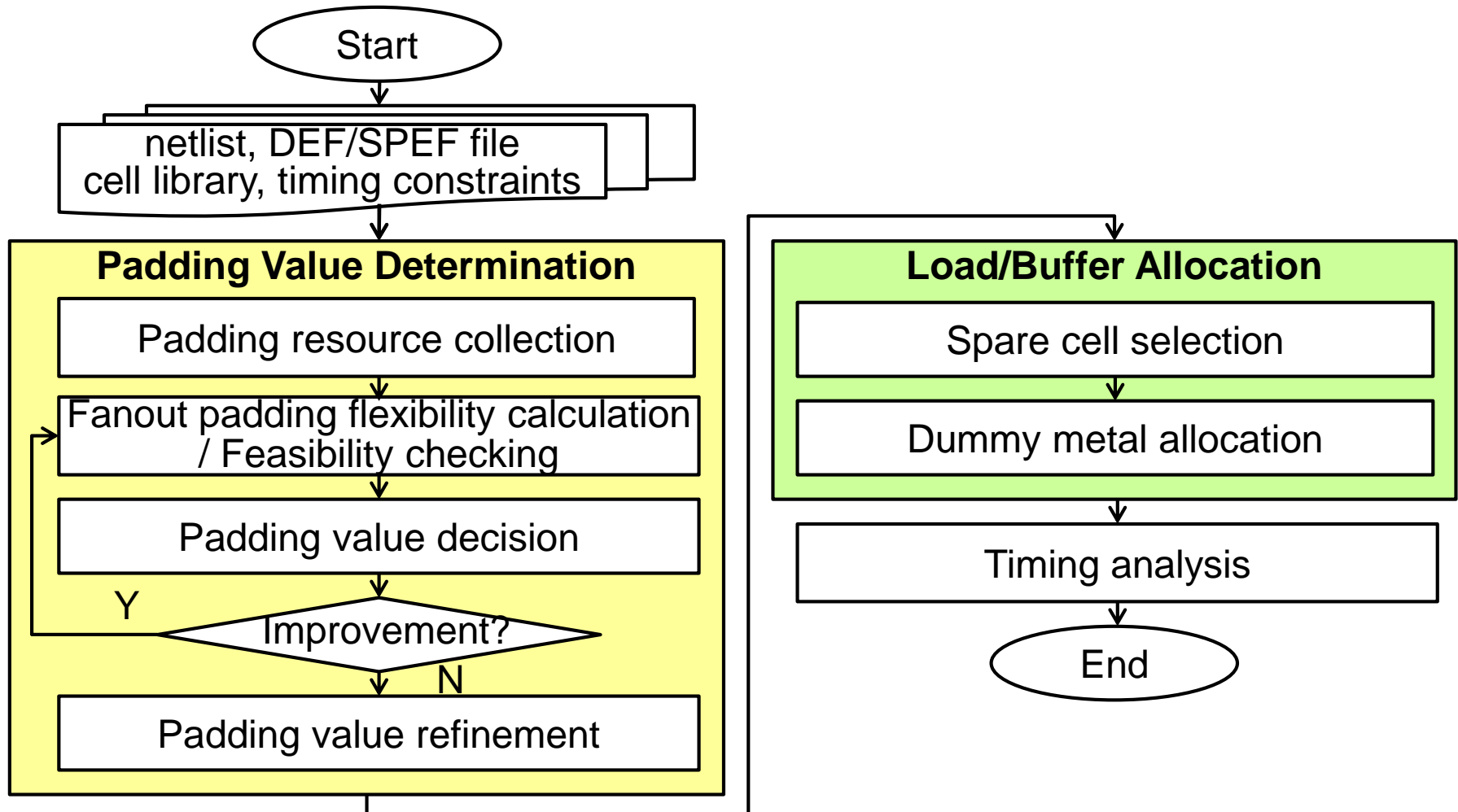
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Overview of PushPull

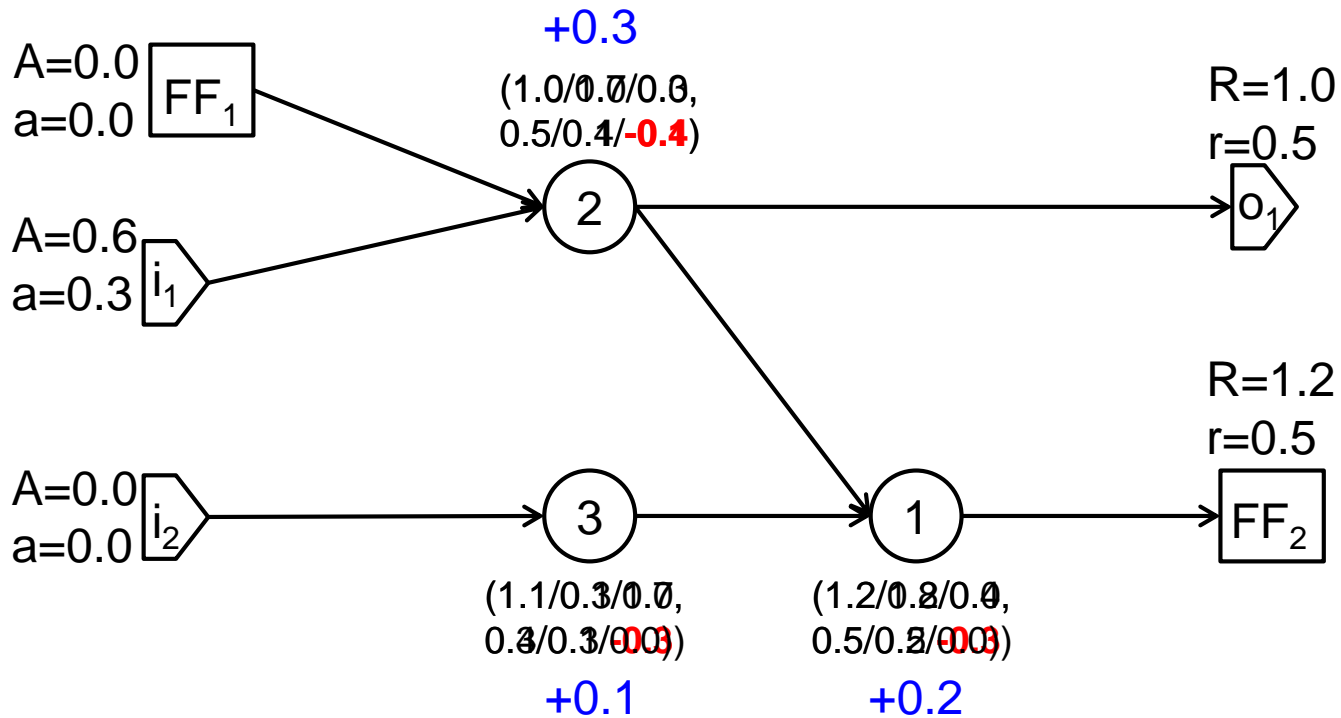
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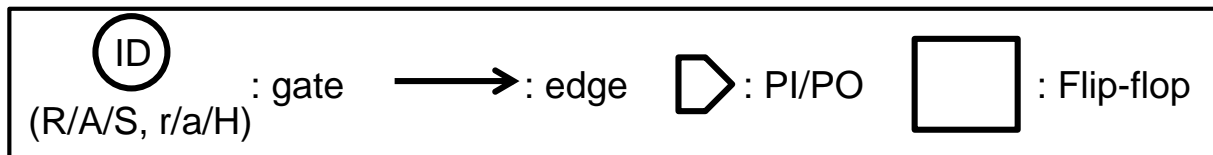
Example: Padding Value Determination

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First, pad gates



Legend:

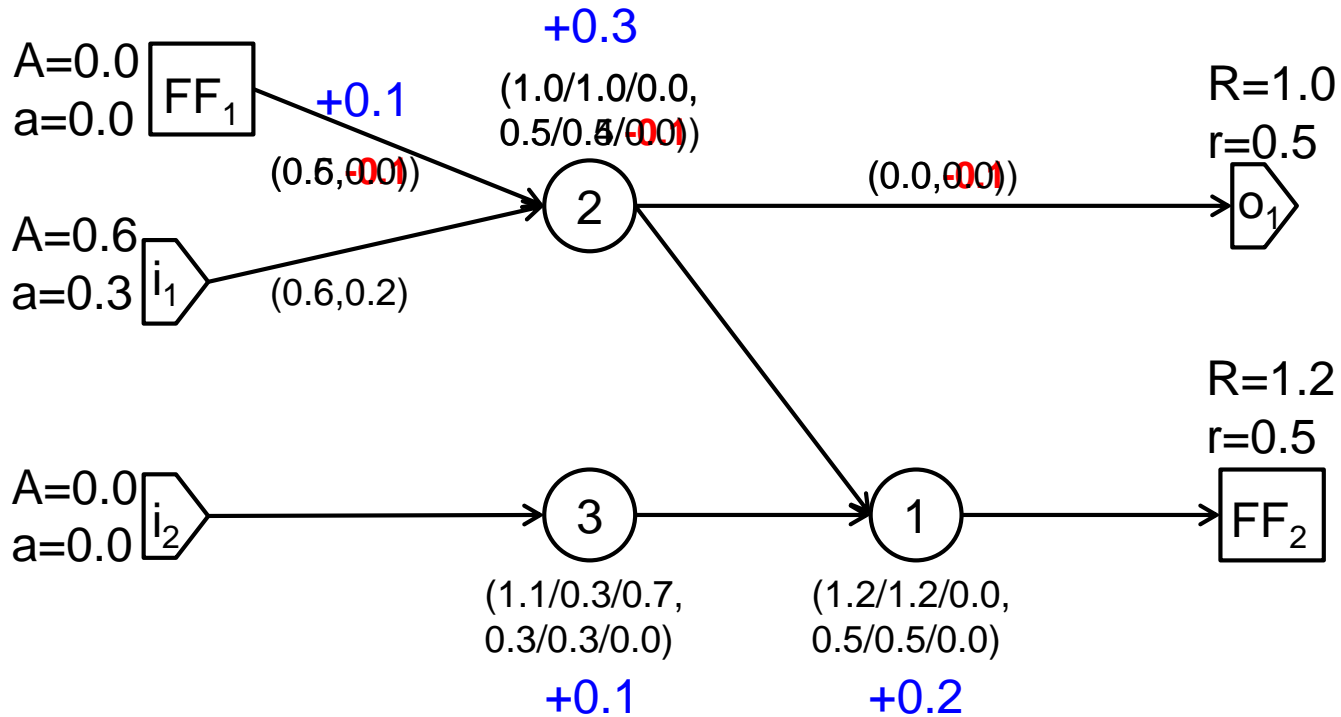


ID	1	2	3
Delay	0.1	0.1	0.1

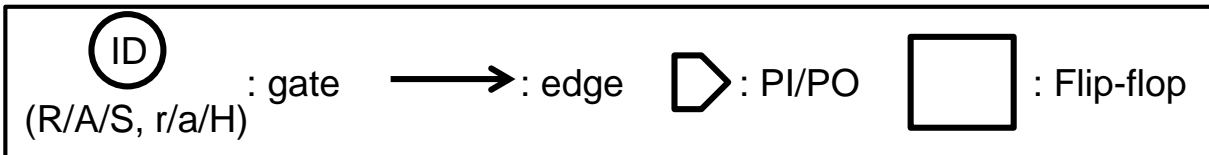
Example: Padding Value Determination

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Second, pad wires



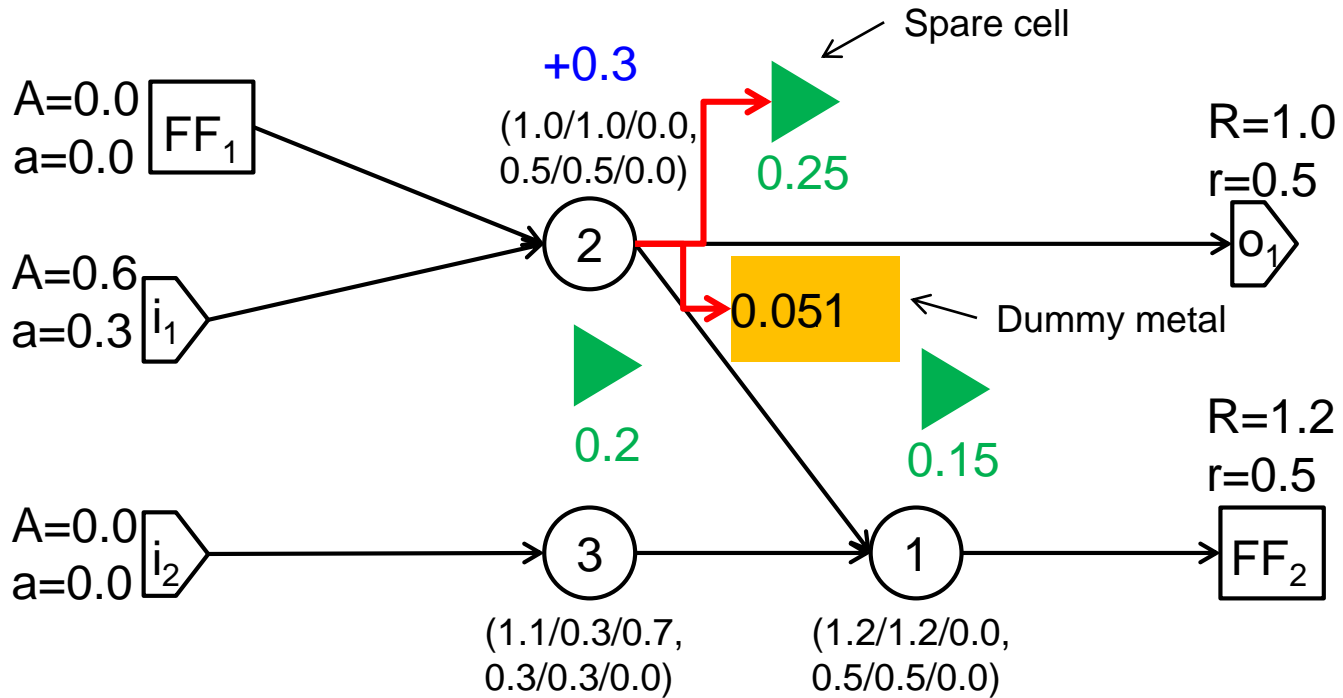
Legend:



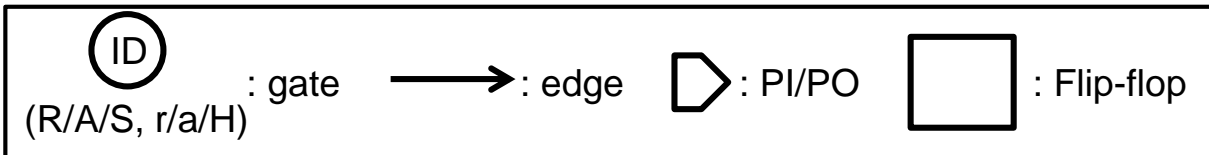
ID	1	2	3
Delay	0.1	0.1	0.1

Example: Load/Buffer Allocation

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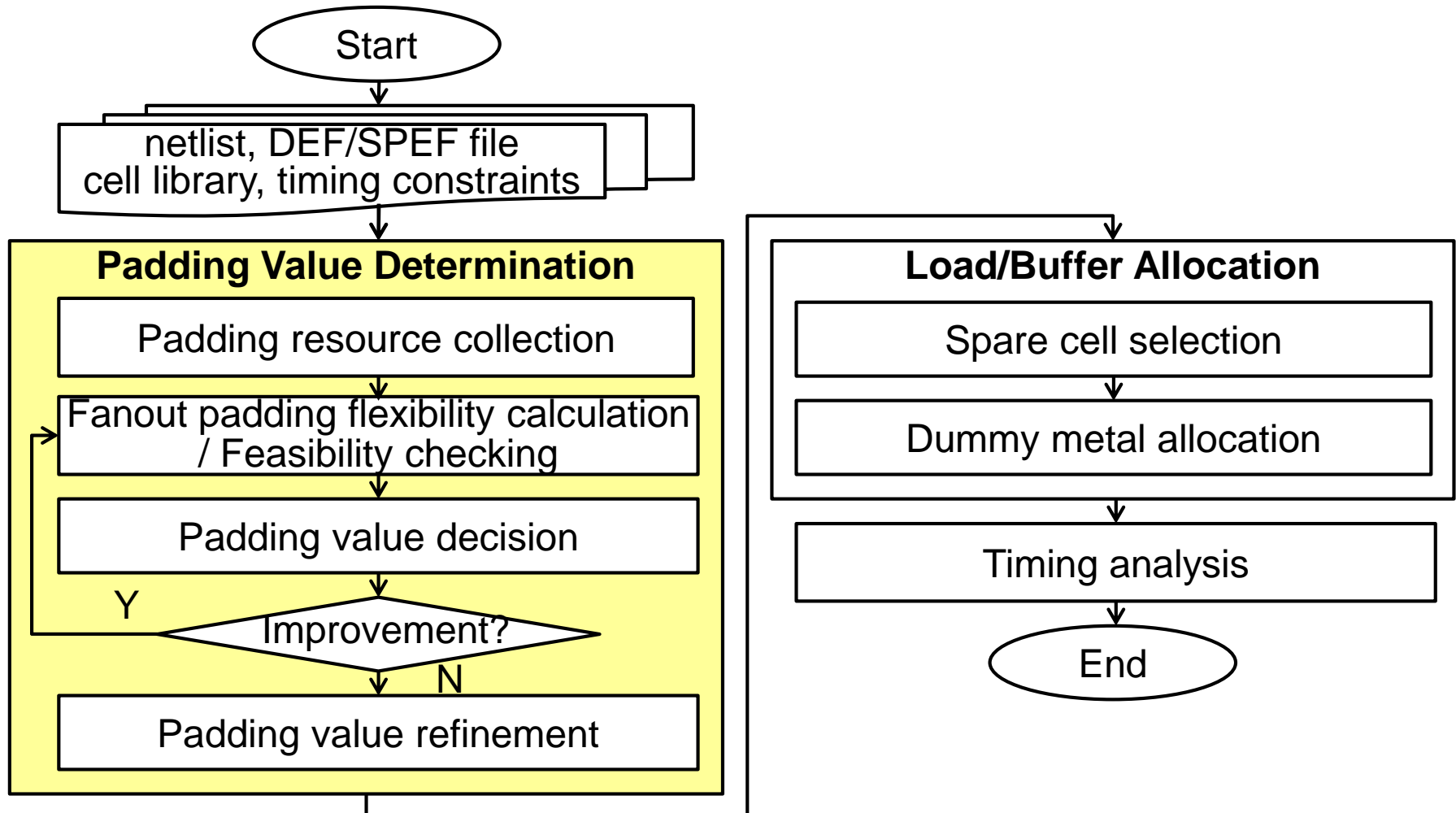
Legend:



ID	1	2	3
Delay	0.1	0.1	0.1

Padding Value Determination

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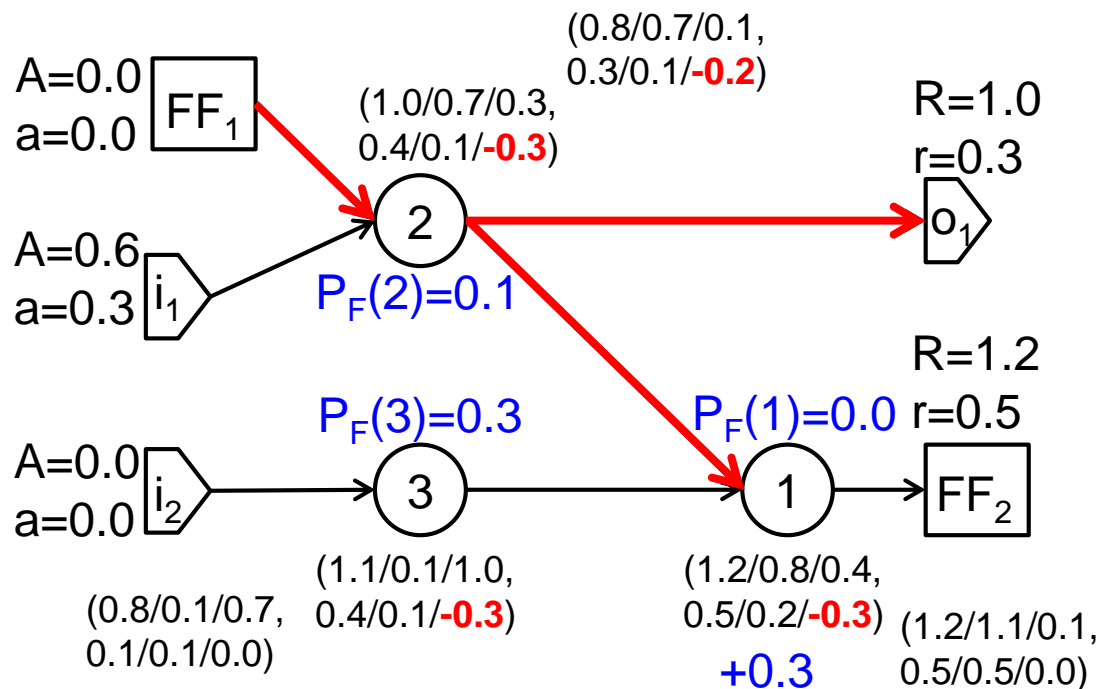


Fanout Padding Flexibility Calculation

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- Fanout padding flexibility $P_F(i)$ of gate i
 - ▣ Reflect the **maximum padding value allowed on its whole fanout cone** with a global view

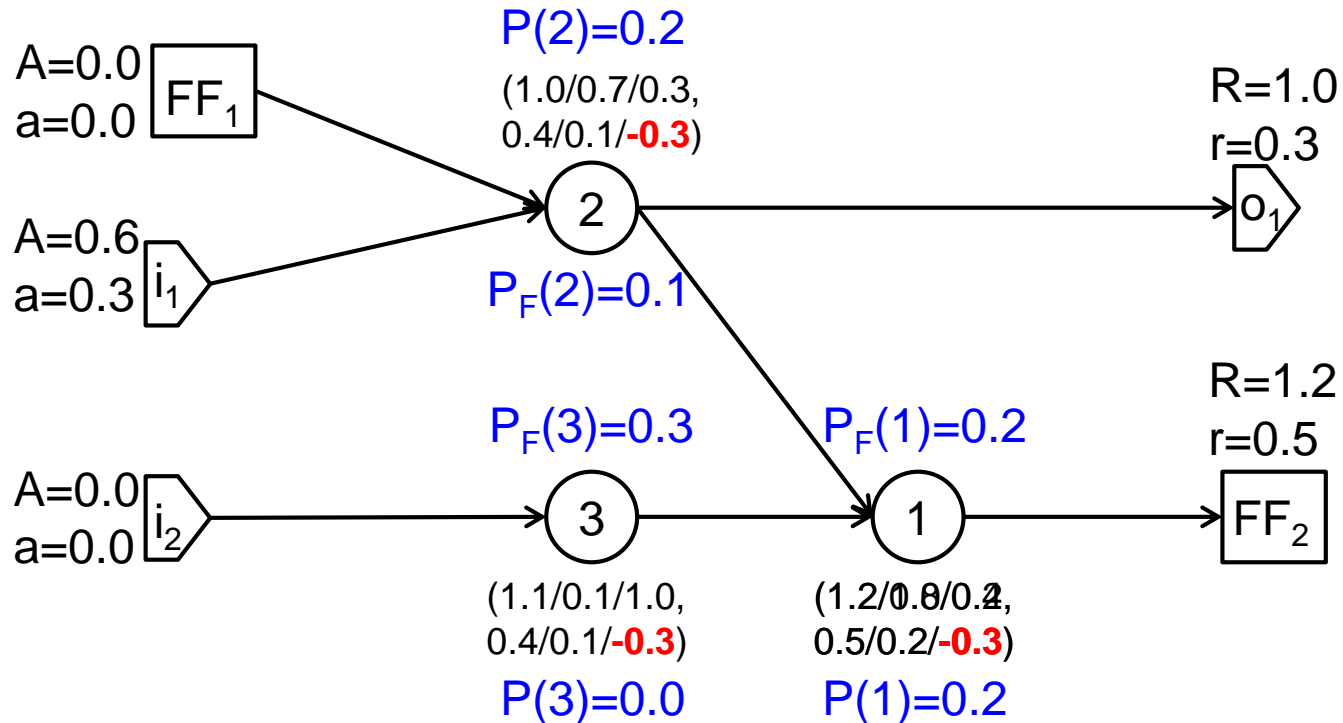
$$P_F(i, j) = \begin{cases} 0, & \text{if } g_i \in PO \text{ or } H(i) \geq 0; \\ \min\{0, \min\{H'(i, j) | e(i, j) \in E\}\} - H(i), & \text{otherwise.} \end{cases}$$



Padding Value Decision

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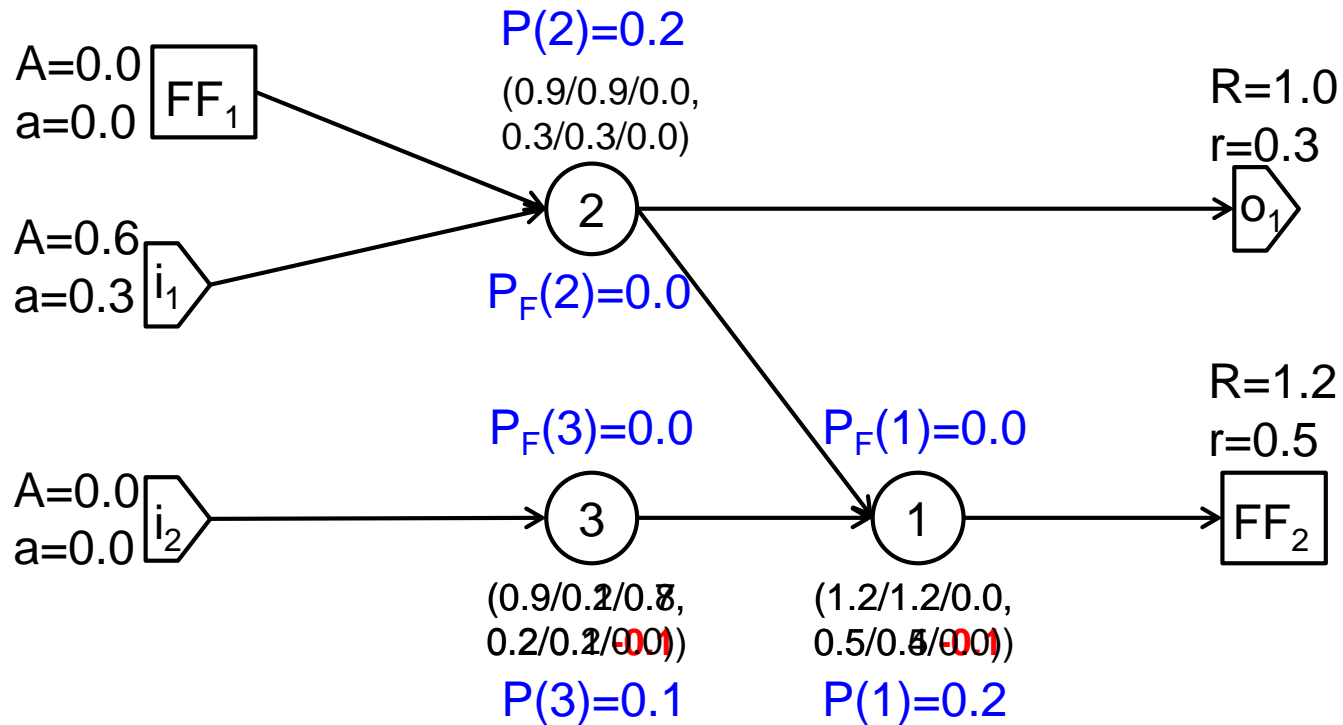
- Decide the padding value of each gate in the topological order
 - ▣ Only pad the remaining slack
 - $P(i) = \max\{P_{saf}(i) - P_F(i), 0\}$



Padding Value Decision

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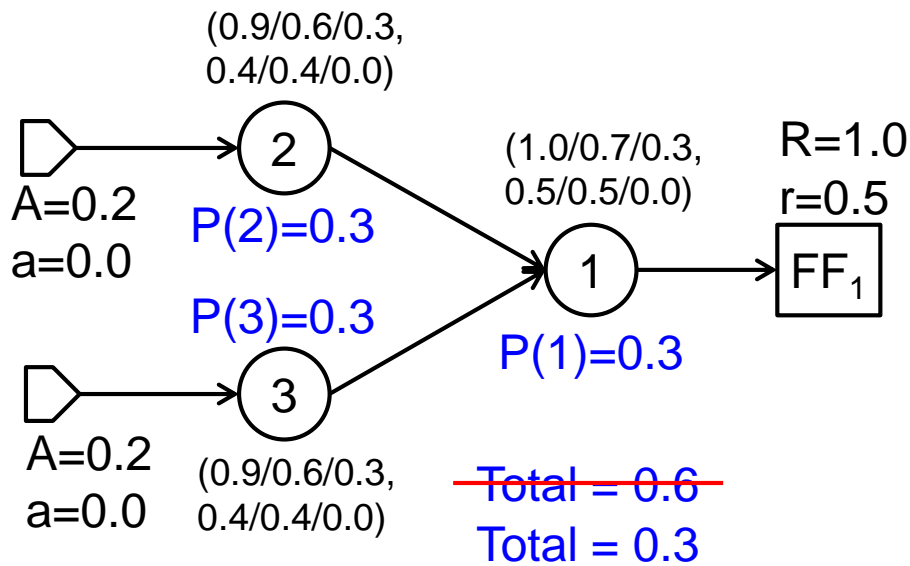
- Iterate until no more improvement



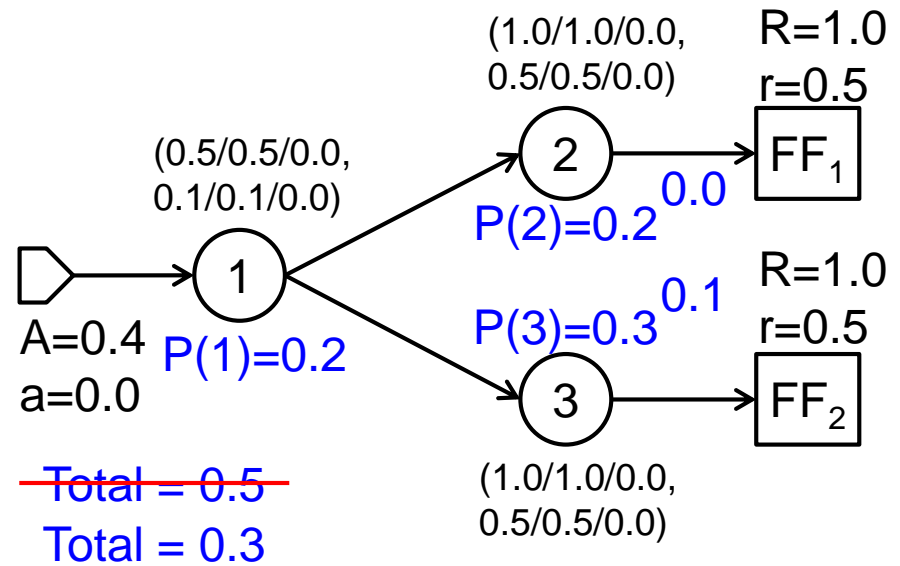
Padding Value Refinement

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- Further reduce the total padding values with forked path
 - Push the padding values toward the gates where two or more paths fork



Joined short paths

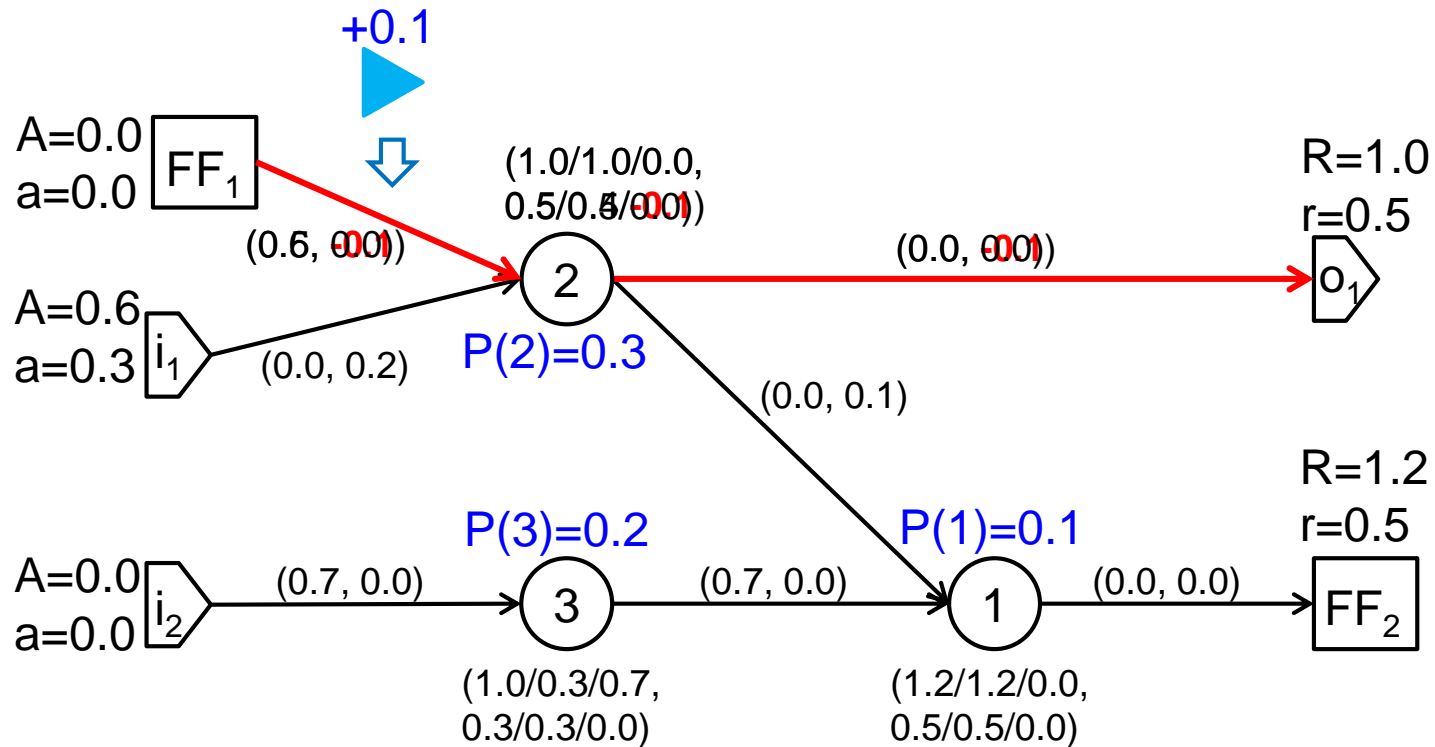


Forked short paths

Buffer Insertion

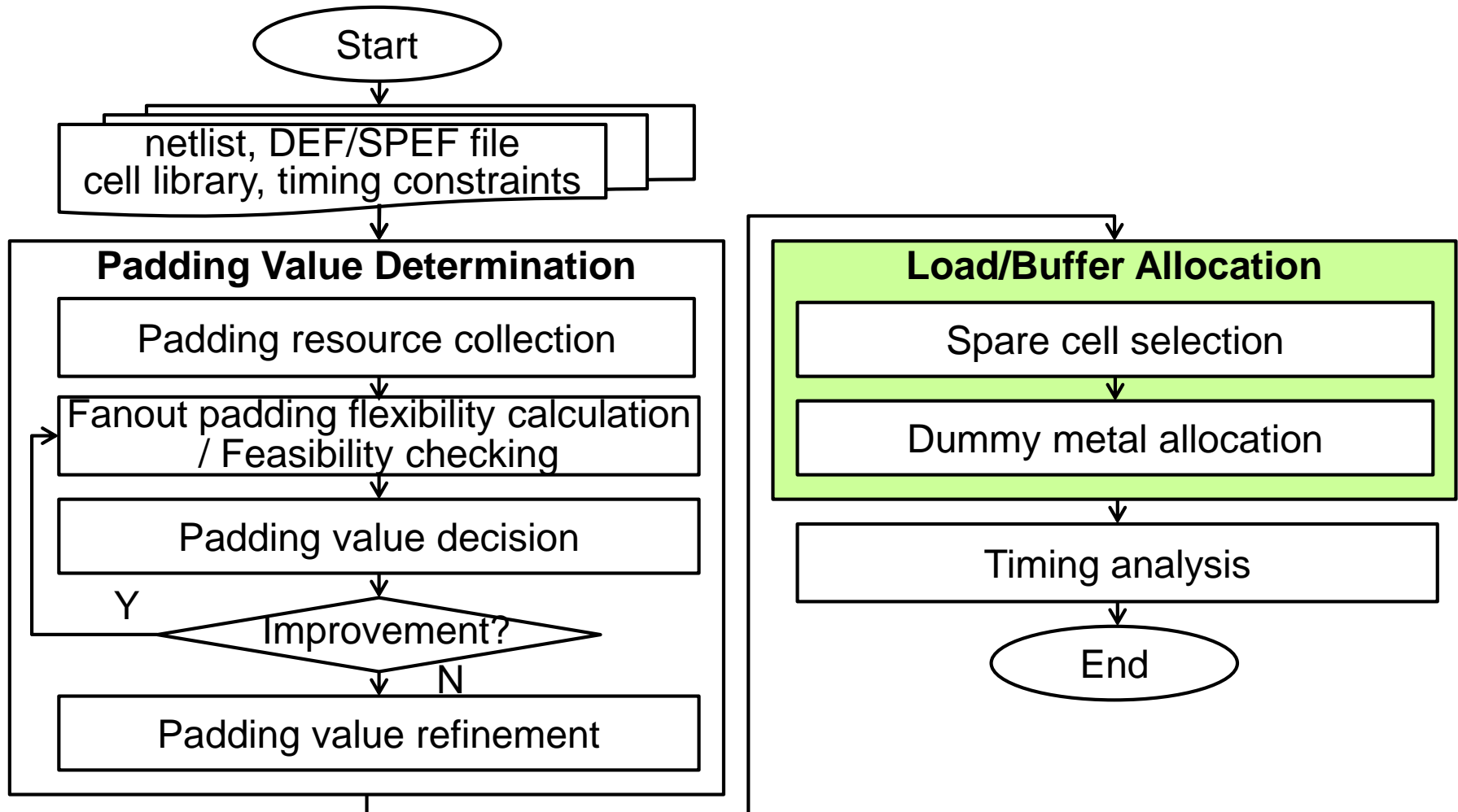
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- When hold violations cannot be fully cleaned by padding on gates
 - ▣ Padding on wires (buffer insertion)



Load/Buffer Allocation

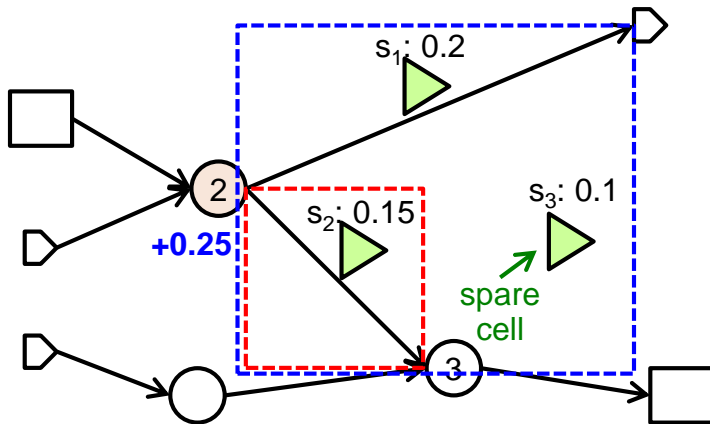
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Spare Cell Selection (1/2)

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- Extract the available spare cells located within the bounding box of its fanout net
- Find suitable spare cell candidates for gate/wire
 - ▣ Reduce to the **subset sum problem**

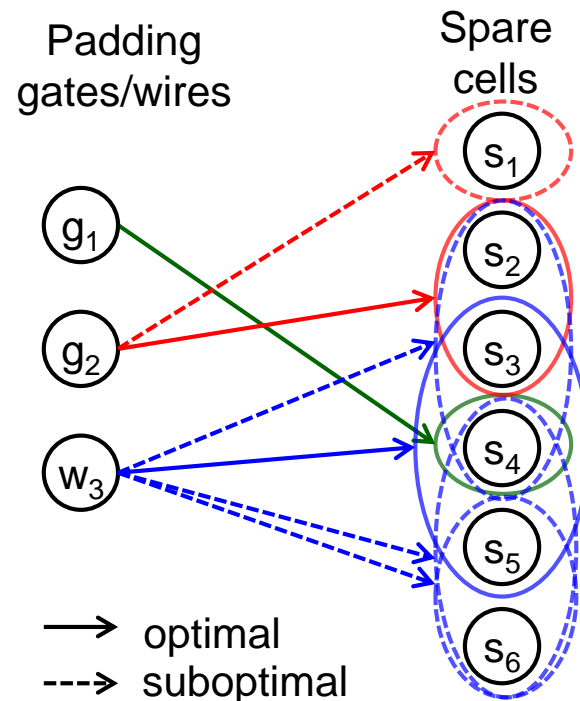
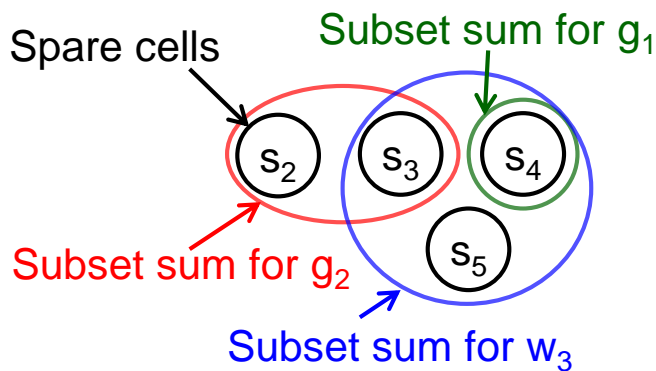


		Padding value					
		0.00	0.05	0.10	0.15	0.20	0.25
Spare cells	\emptyset	0.00 \emptyset	0.00 \emptyset	0.00 \emptyset	0.00 \emptyset	0.00 \emptyset	0.00 \emptyset
	$\{s_1\}$	0.00 \emptyset	0.00 \emptyset	0.00 \emptyset	0.00 \emptyset	0.20 $\{s_1\}$	0.20 $\{s_1\}$
	$\{s_1, s_2\}$	0.00 \emptyset	0.0 \emptyset	0.00 \emptyset	0.15 $\{s_2\}$	0.20 $\{s_1\}$	0.20 $\{s_1\}$
	$\{s_1, s_2, s_3\}$	0.00 \emptyset	0.0 \emptyset	0.10 $\{s_3\}$	0.15 $\{s_2\}$	0.20 $\{s_1\}$	0.25 $\{s_2, s_3\}$

Spare Cell Selection (2/2)

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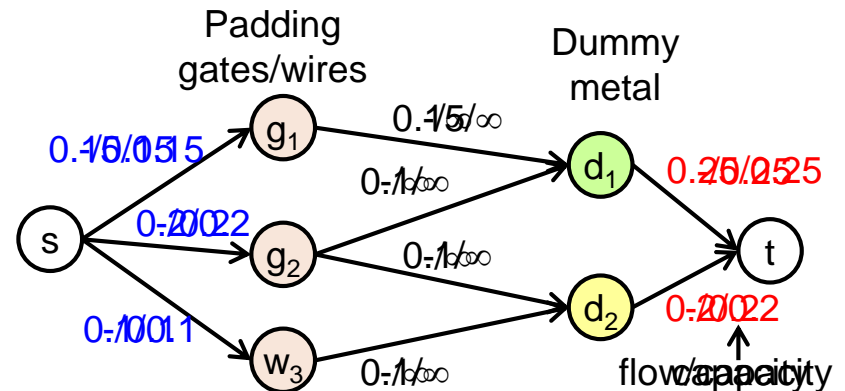
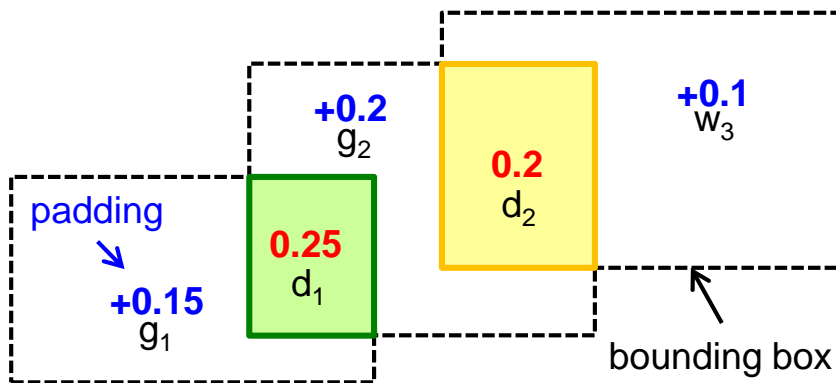
- **Solve the competition problem between different padding gates/wires**
 - ▣ Record multiple subset sum solutions
 - ▣ Sort the gates/wires in ascending order of the number of spare cell solutions
 - ▣ Assign the gates/wires to their best solution in the sorted order



Dummy Metal Allocation

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- Fix remaining padding by dummy metal insertion
 - ▣ Convert the delay to an amount of capacitance
 - ▣ Assign un-overlapped metal resource
 - ▣ Resort the unfixed padding to maximum network flow



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Experimental Results

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- Platform: Intel® Xeon® CPU E5620 @ 2.40GHz with 16GB memory, CentOS 5.5
- Compare with two greedy heuristics

Circuit	Ours: PushPull					Greedy 1: Largest setup first [2]					Greedy 2: Most path sharing first [1][2][3]				
	TNS ₁ (ps)	THS ₁ (ps)	Padding delay (ps)	#lts.	Runtime (s)	TNS ₁ (ps)	THS ₁ (ps)	Padding delay (ps)	#lts.	Runtime (s)	TNS ₁ (ps)	THS ₁ (ps)	Padding delay (ps)	#lts.	Runtime (s)
s1196	0.0	0.0	152.5	1	0.02	0.0	0.0	338.4	5	0.02	0.0	0.0	173.8	3	0.01
s1423	0.0	0.0	4,746.9	2	0.05	0.0	43.5	4,968.7	56	0.45	0.0	43.5	4,802.8	35	0.24
s5378	0.0	0.0	3,722.7	2	0.08	0.0	79.3	4,678.1	60	0.79	0.0	79.3	4,555.4	43	0.58
s9234	0.0	0.0	1,647.5	1	0.05	0.0	12.0	1,878.3	33	0.30	0.0	12.0	2,158.5	27	0.26
s13207	0.0	0.0	371.2	2	0.07	0.0	34.5	762.3	22	0.21	0.0	34.5	621.5	18	0.21
s15850	0.0	0.0	1,510.8	2	0.04	0.0	0.0	1,662.8	43	0.25	0.0	0.0	2,161.5	41	0.27
s38584	0.0	0.0	143,764.1	2	1.04	0.0	0.0	225,026.0	780	115.19	0.0	85.8	130,703.0	512	80.37
des_perf	0.0	0.0	583,579.0	2	9.46	0.0	19,270.5	795,022.0	3,414	6,401.86	0.0	3,864.1	595,088.0	2,257	4,202.46
b19	0.0	0.0	1,675,688.0	4	21.68	0.0	108,078.0	6,128,710.0	21,902	37,473.30	0.0	65,746.7	1,729,230.0	6,220	10,978.40

TNS₁: total negative setup slack after padding value determination.

THS₁: total negative hold slack after padding value determination.

[1] S. Yoshikawa, "Hold time error correction method and correction program for integrated circuits," US Patent 6,990,646, 2006.

[2] Y. Sun et al., "Method and apparatus for fixing hold time violations in a circuit design," US Patent 7,278,126, 2007.

[3] Y. Liu et al., "Re-synthesis for cost-efficient circuit-level timing speculation," DAC, pp. 158–163, 2011.

Experimental Results (cont'd)

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□ Compare with LP solutions

Circuit	#Gate	#FF	#SFF	Conservative clock period (ns)	THS (ps)	LP				Ours: PushPull					
						TNS ₁ (ps)	THS ₁ (ps)	Padding delay (ps)	Runtime (s)	TNS ₁ (ps)	THS ₁ (ps)	Padding delay (ps)	Normalized to LP	#Ite.	Runtime (s)
s1196	301	19	1	1.0	152.5	0.0	0.0	152.5	0.03	0.0	0.0	152.5	1.00	1	0.02
s1423	486	74	45	1.0	4,916.9	0.0	0.0	4,126.8	0.15	0.0	0.0	4,746.9	1.15	2	0.05
s5378	739	162	37	1.0	3,852.8	0.0	0.0	3,661.3	0.06	0.0	0.0	3,722.7	1.02	2	0.08
s9234	555	132	24	1.0	1,929.0	0.0	0.0	1,459.6	0.05	0.0	0.0	1,647.5	1.13	1	0.05
s13207	748	213	14	1.0	371.2	0.0	0.0	371.2	0.03	0.0	0.0	371.2	1.00	2	0.07
s15850	428	128	29	1.0	2,114.6	0.0	0.0	1,305.1	0.03	0.0	0.0	1,510.8	1.16	2	0.04
s38584	7,890	1,159	194	3.4	108,759.0	0.0	0.0	108,476.0	6.96	0.0	0.0	143,764.1	1.33	2	1.04
des_perf	51,349	8,808	1,190	2.9	583,579.0	0.0	0.0	583,579.0	60.59	0.0	0.0	583,579.0	1.00	2	9.46
b19	72,872	5,541	2,737	3.8	1,481,800.0	NA	NA	NA	timeout	0.0	0.0	1,675,688.0	-	4	21.68

TNS₁: total negative setup slack after padding value determination.

THS₁: total negative hold slack after padding value determination.

□ The impact of input slew on padding delay capacitance conversion

- The average error rate over all cases is only 0.56%.

Experimental Results (cont'd)

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- Compare our load/buffer allocation method with LP+Mapping

Circuit	LP+Mapping			Ours: PushPull		
	TNS ₂ (ps)	THS ₂ (ps)	Runtime (s)	TNS ₂ (ps)	THS ₂ (ps)	Runtime (s)
s1196	0.0	0.3	0.03	0.0	0.0	0.33
s1423	0.0	826.4	0.09	0.0	0.0	0.43
s5378	0.0	302.3	0.05	0.0	0.0	0.54
s9234	0.0	631.3	0.04	0.0	0.0	0.41
s13207	0.0	161.2	0.03	0.0	0.0	0.61
s15850	0.0	352.0	0.02	0.0	0.0	0.38
s38584	0.0	29,970.7	0.58	0.0	0.0	1.96
des_perf	0.0	51,146.0	41.99	0.0	0.0	12.36
b19	NA	NA	NA	0.0	0.0	43.33

TNS₂: total negative setup slack after load/buffer allocation.

THS₂: total negative hold slack after load/buffer allocation.

Conclusion

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- **Focus on the severe short path padding problem in resilient circuits**
 - ▣ Enable the timing error detection and correction mechanism of resilient circuits

- **Determine the padding values and locations with a global view**
 - ▣ vs. the local view adopted by recent prior work

- **Realize the determined padding values at physical implementation**
 - ▣ Propose coarse-grained and fine-grained load/buffer allocation by using spare cells and dummy metal

Future Work

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- **Allocate spare cell and dummy metal simultaneously**
 - ▣ Spare cells: discrete capacitance resource
 - ▣ Dummy metal: continuous capacitance resource

- **Adopt Composite Current Source (CCS) timing model**
 - ▣ Use more accuracy delay model

Thank You!

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Backup Slides

The Resilient Circuit Design Flow

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